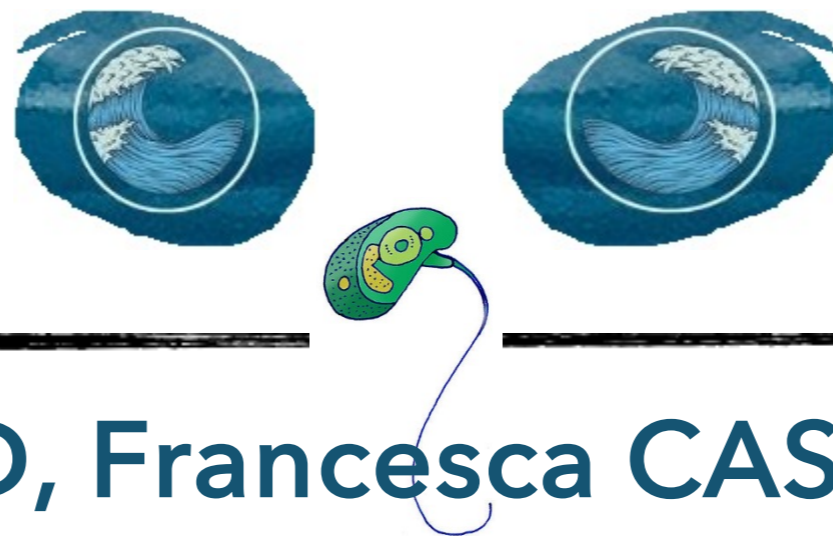


Effect of temperature and light on phytoplankton growth

Océania



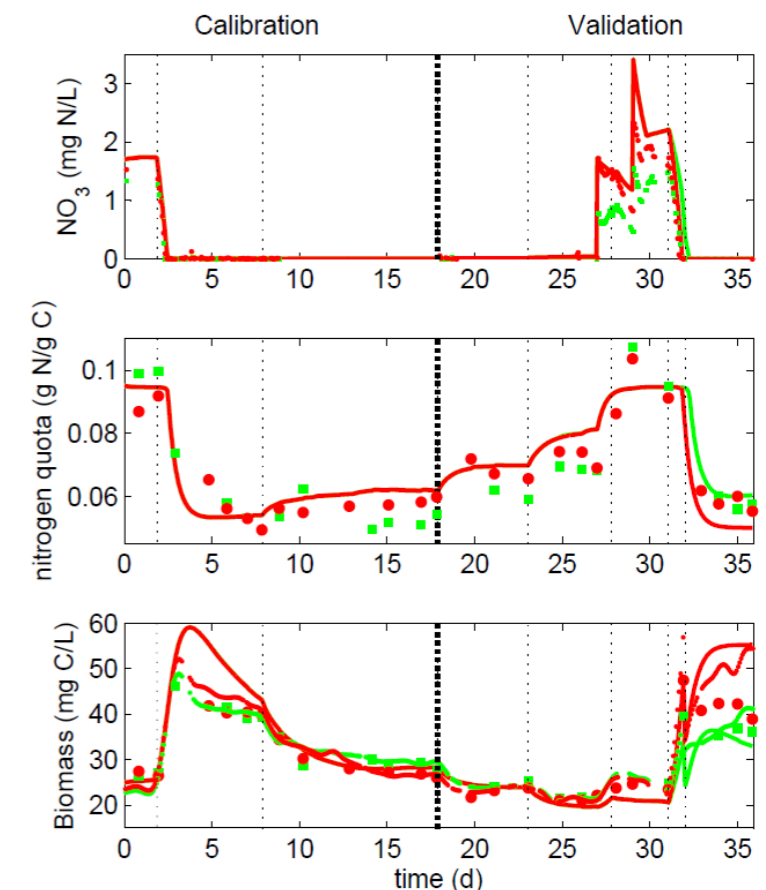
Olivier BERNARD, Francesca CASAGLI, Romain RANINI, Ignacio FIERRO, Jineth ARANGO, Kilian BURGI, David JEISON, Antoine SCIANDRA, Lionel GUIDI



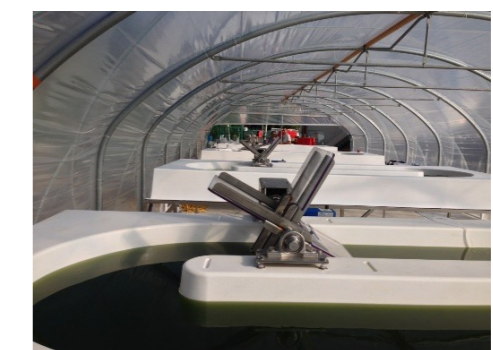
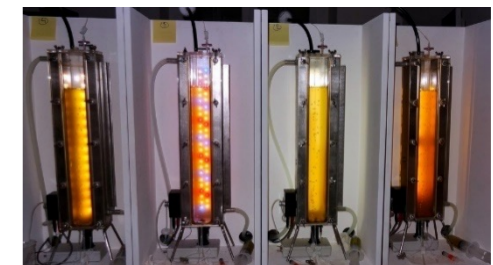
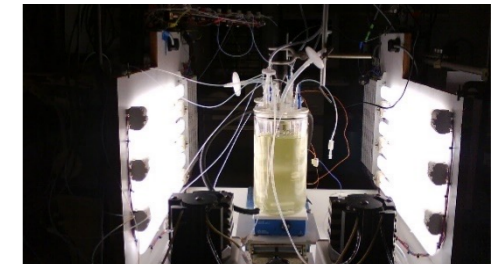
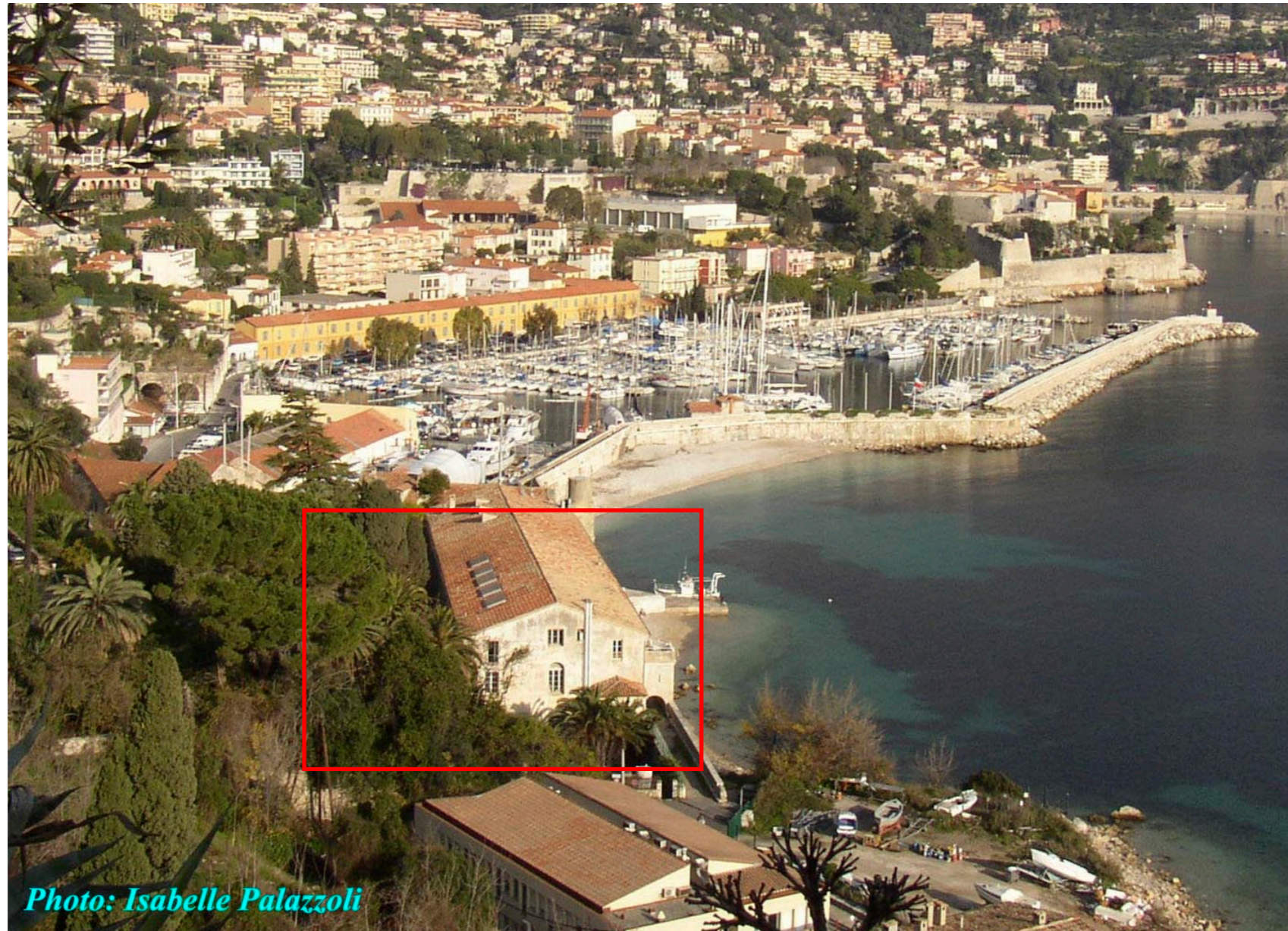
Biological control of artificial ecosystems: modelling, control and optimization. Focus on phytoplankton.

$$(D) \begin{cases} \dot{s} = Ds_{in} - \rho(s)x - Ds \\ \dot{q} = \rho(s) - \mu(q)q \\ \dot{x} = \mu(q)x - Dx \end{cases}$$

$$\begin{aligned} \text{Uptake rate: } \rho(s) &= \rho_m \frac{s}{s + K_s} \\ \text{Growth rate: } \mu(q) &= \bar{\mu} \left(1 - \frac{Q_0}{q}\right) \end{aligned}$$



Biocore: joined team with the Oceanographic Laboratory from Villefranche (LOV)



Link to in situ campaigns



Lionel GUIDI



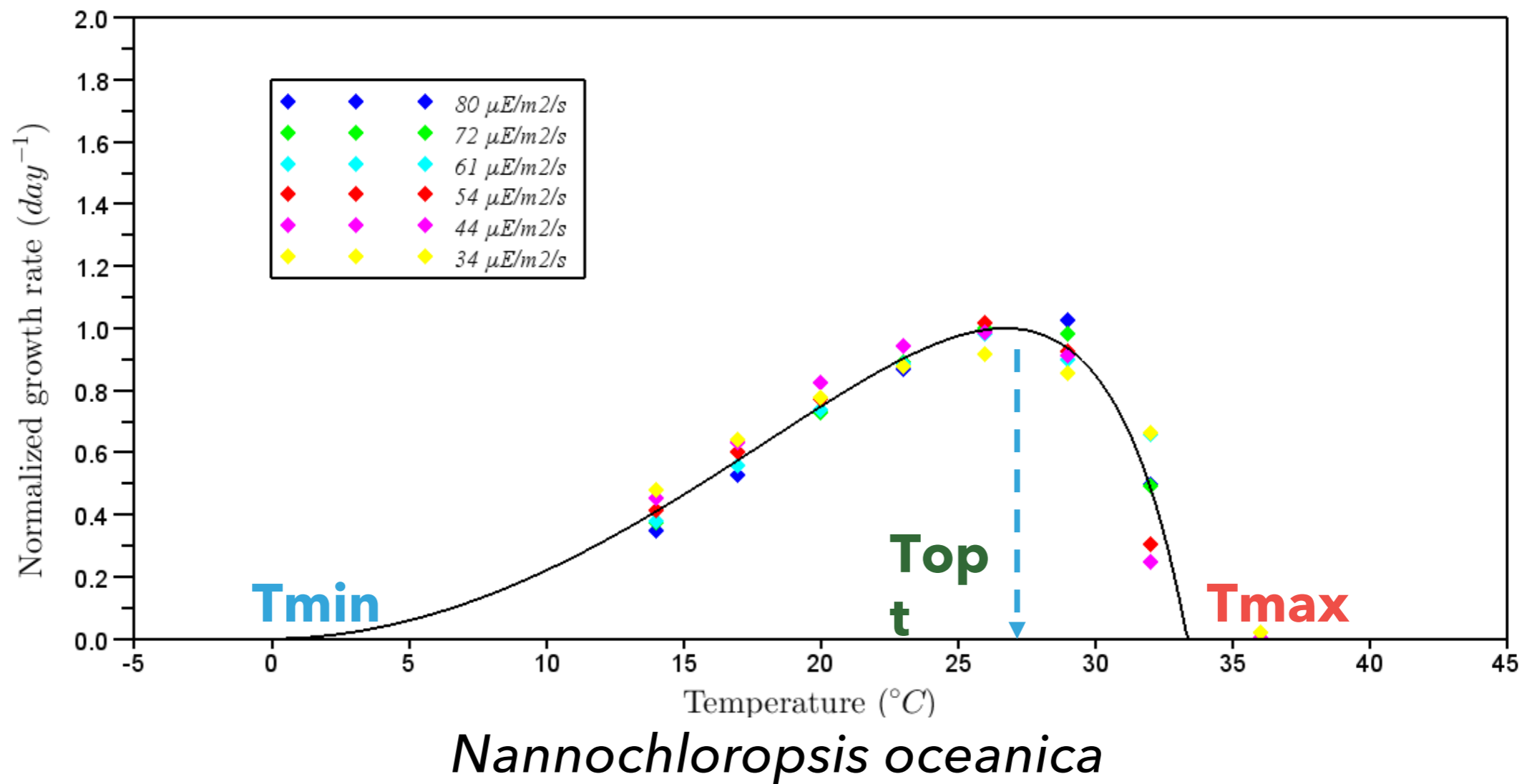
OCEANIA

- Understanding the rules driving response to temperature in phytoplankton (O. Bernard)
- Neural ODE for representing phytoplankton growth driven by light (I. Fierro)
- Towards hybrid modelling of artificial microbial ecosystems (F. Casagli)
- Spatio-temporal high-resolution models of particulate organic matter abundance in the ocean (R. Ranini)

MICROBIAL RESPONSE TO TEMPERATURE

Temperature impact on growth at various light intensities

Temperature response for most of phytoplankton species

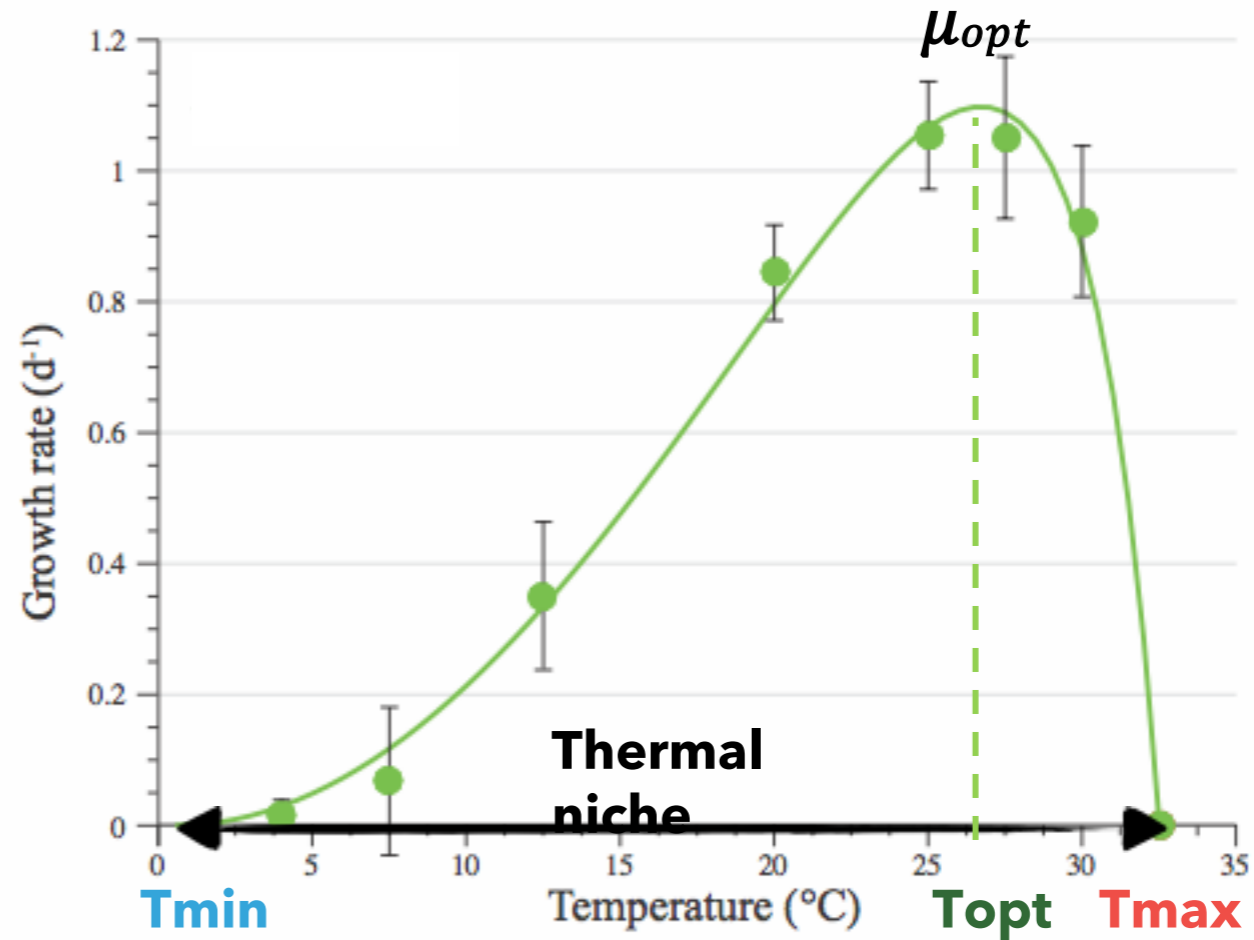


Modelling growth response to temperature

BR model

Cardinal Parameters

T_{min} T_{opt} T_{max} μ_{opt}

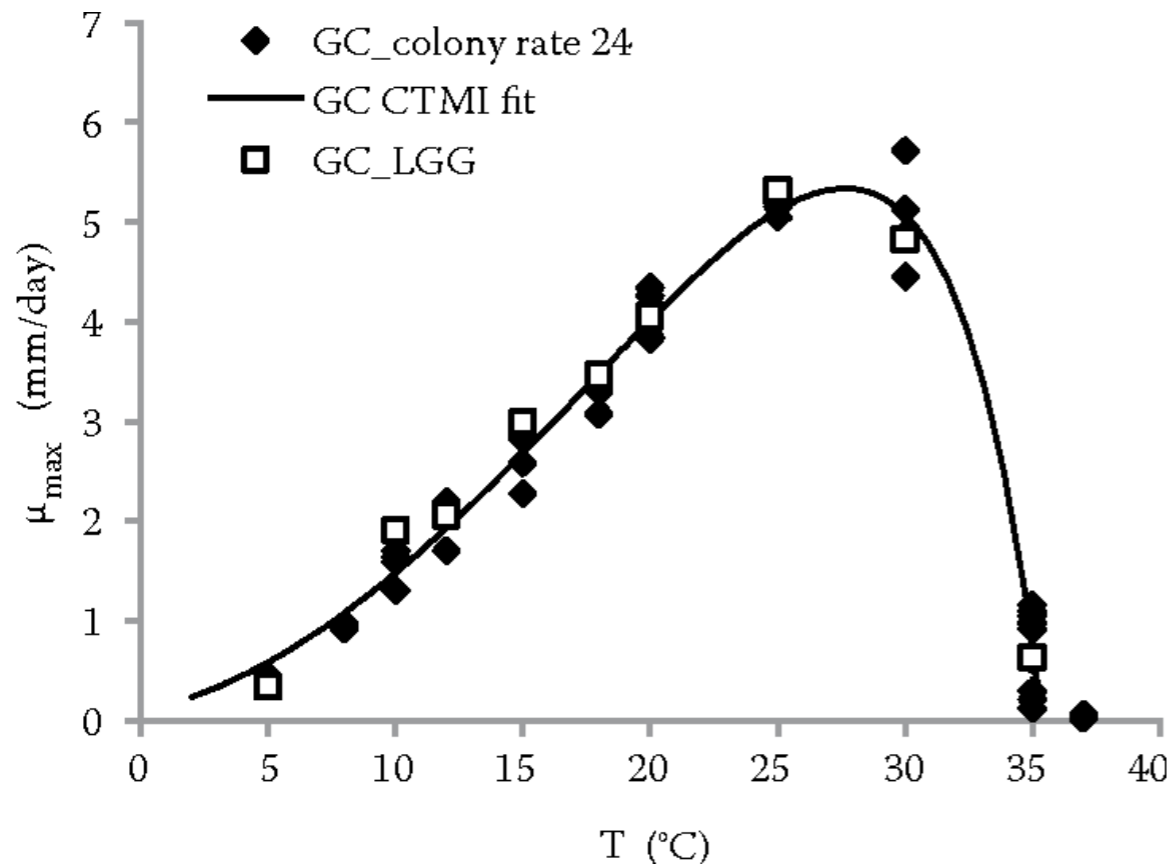


$$\mu_{max} = \begin{cases} 0 & \text{for } T < T_{min} \\ \mu_{opt} \cdot \phi(T) & \text{for } T_{min} < T < T_{max}, \\ 0 & \text{for } T > T_{max}, \end{cases}$$

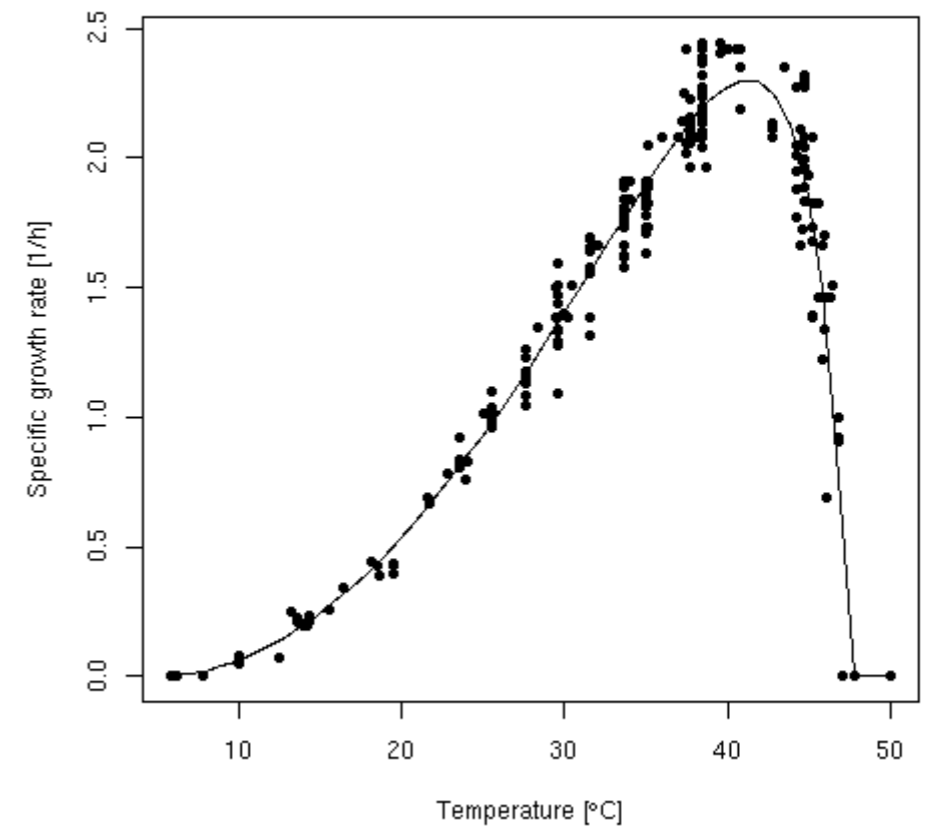
where

$$\phi(T) = \frac{(T - T_{max})(T - T_{min})^2}{(T_{opt} - T_{min})[(T_{opt} - T_{min})(T - T_{opt}) - (T_{opt} - T_{max})(T_{opt} + T_{min} - 2T)]}$$

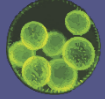
Idem for most of the microorganisms



Geotrichum candidum.(Hudecova et al., 2018)



E. Coli (Lobry& Chessel, 2003)

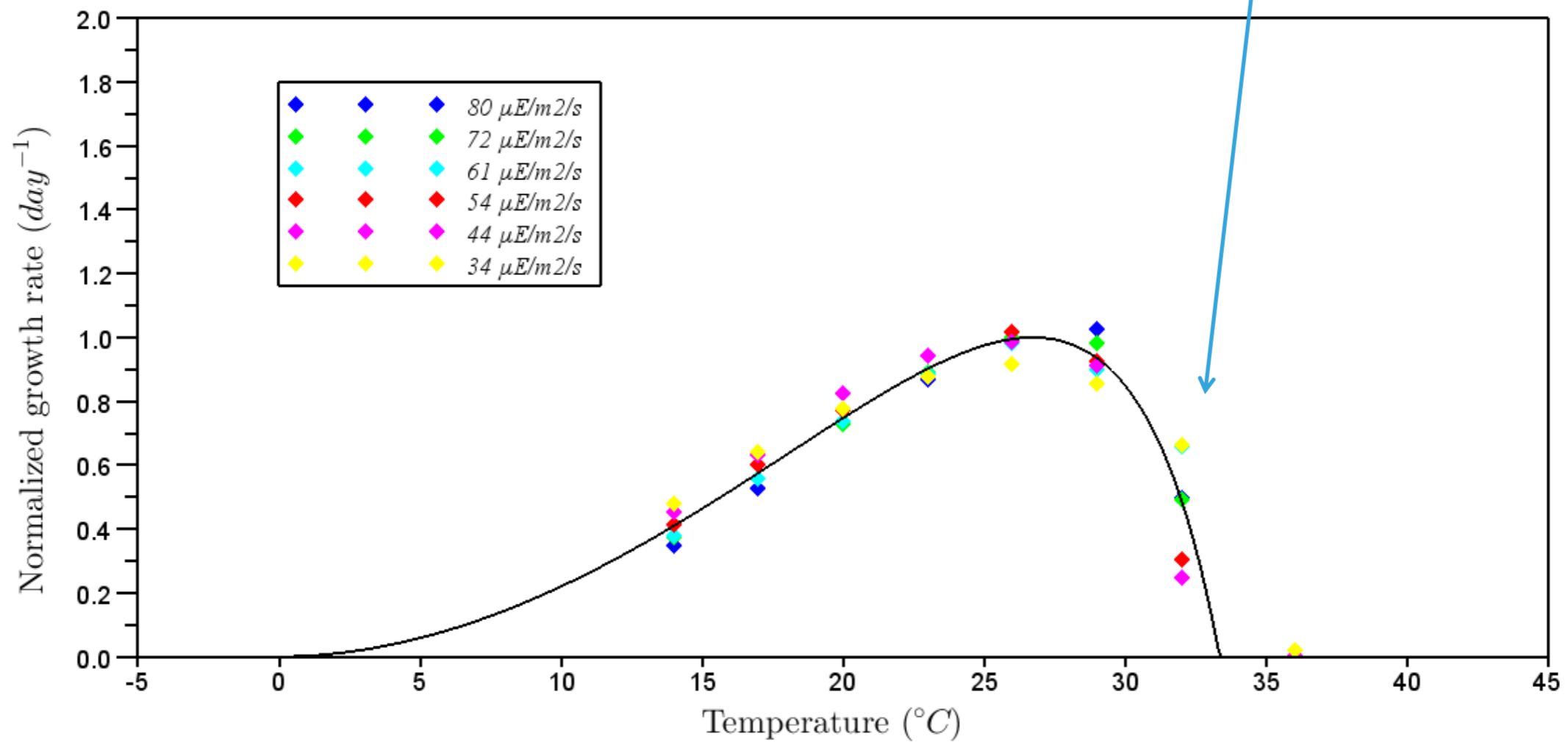


WHICH BIOLOGICAL MECHANISMS INVOLVED?



What happens at high temperature?

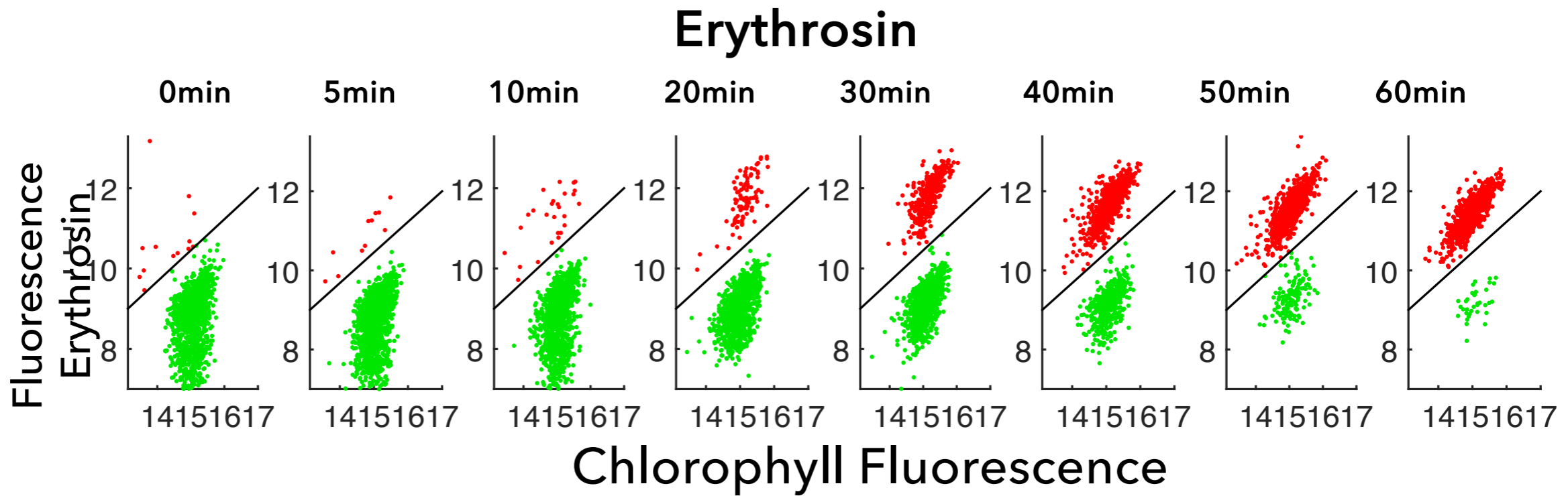
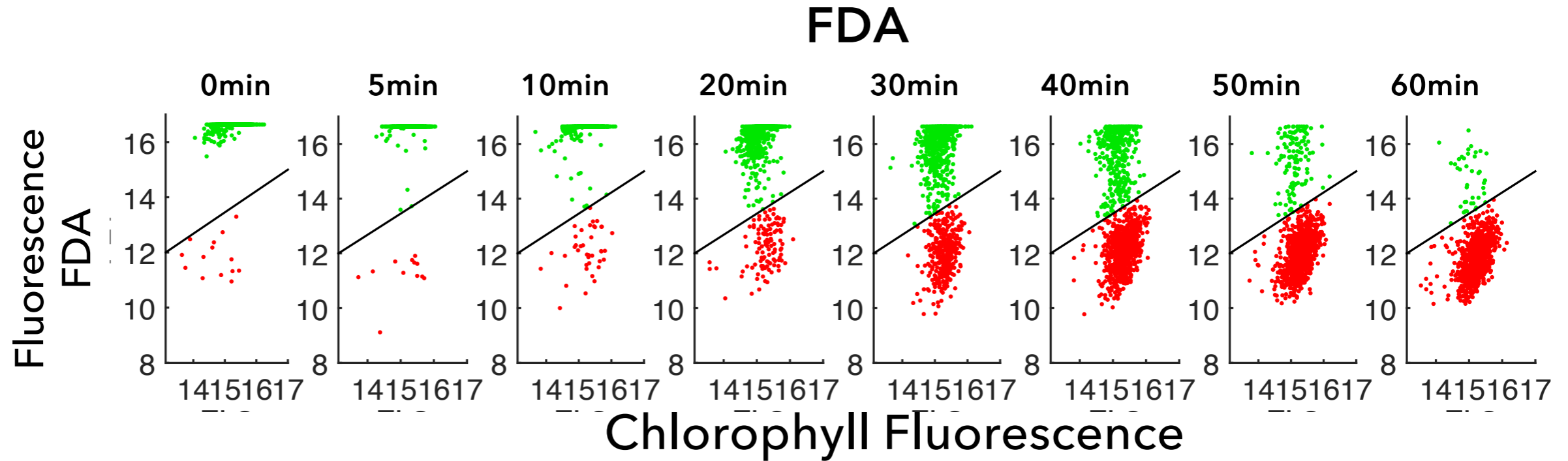
Why is the temperature response dropping?



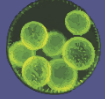
Nannochloropsis oceanica



Océania



Dunaliella salina



ARE THERE SOME GENERAL PATTERNS HIDDEN BEHIND TEMPERATURE RESPONSE?

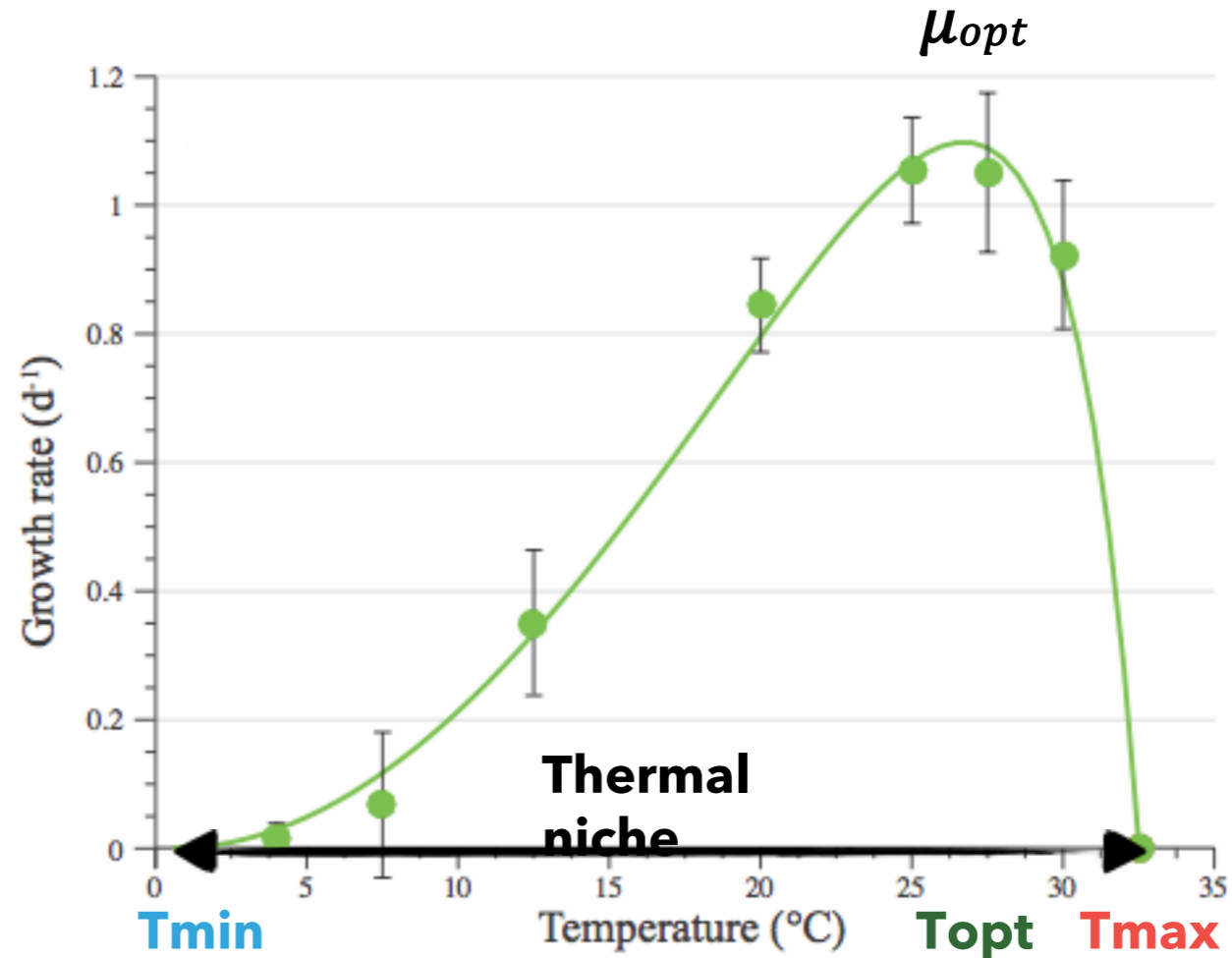
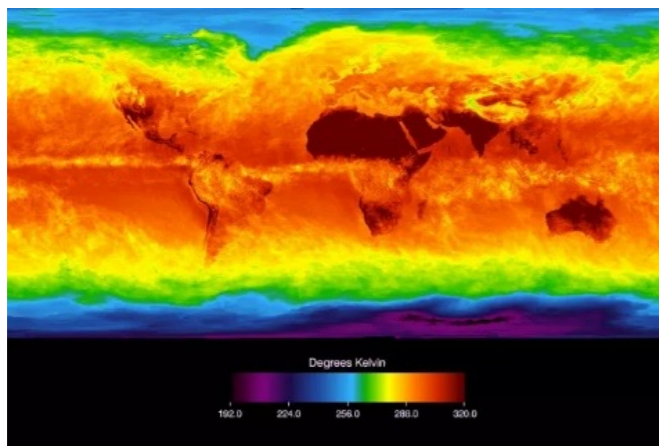
Can we predict the evolution of the Temperature Response?



Link between isolation temperature and the cardinal parameters?

Cardinal Parameters

T_{min} T_{opt} T_{max} μ_{opt}



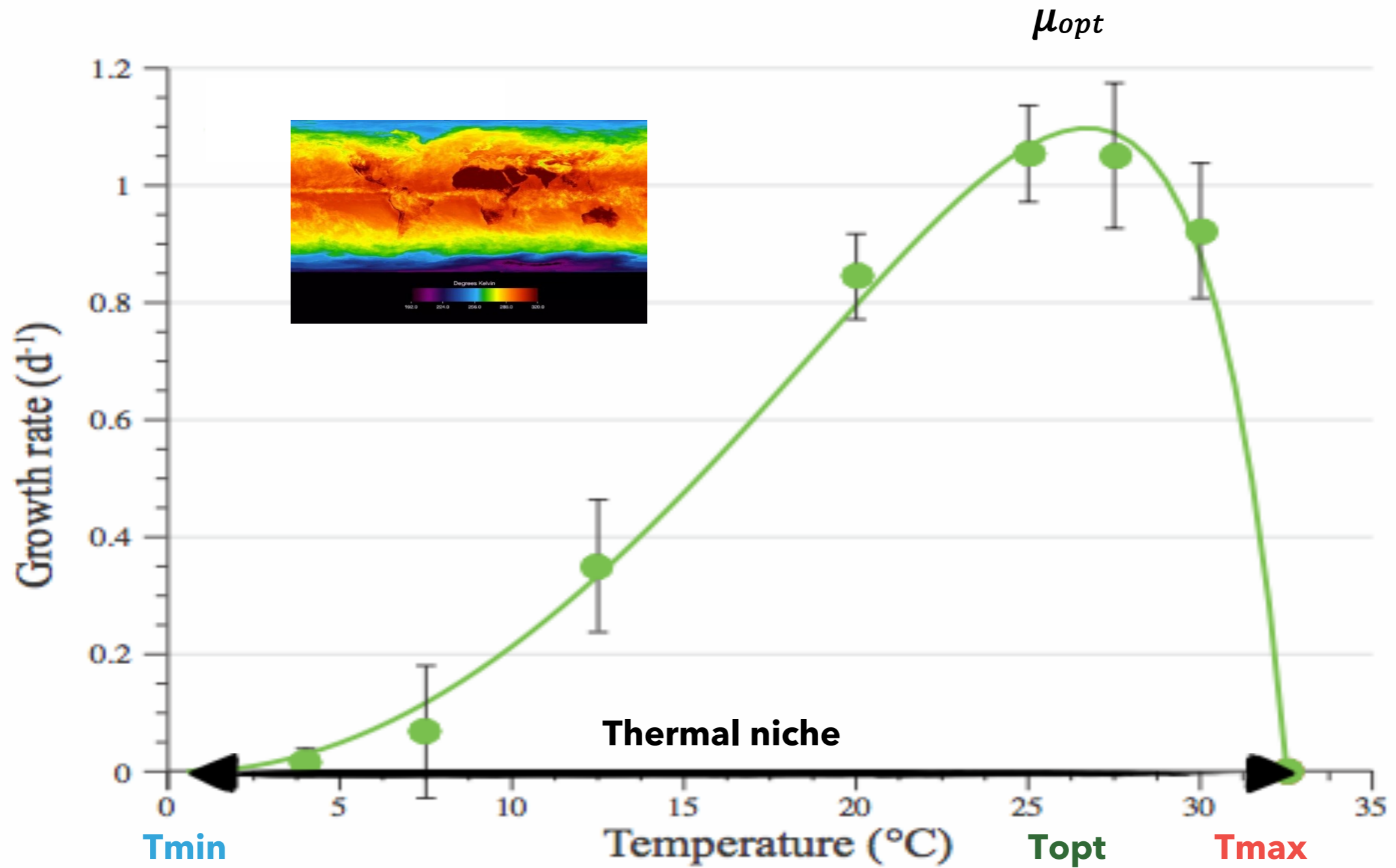
Analysis of 2240 experimental growth rates (merging 3 data bases)

(Thomas, 2016; Corkrey, 2019; Homemade 2020)

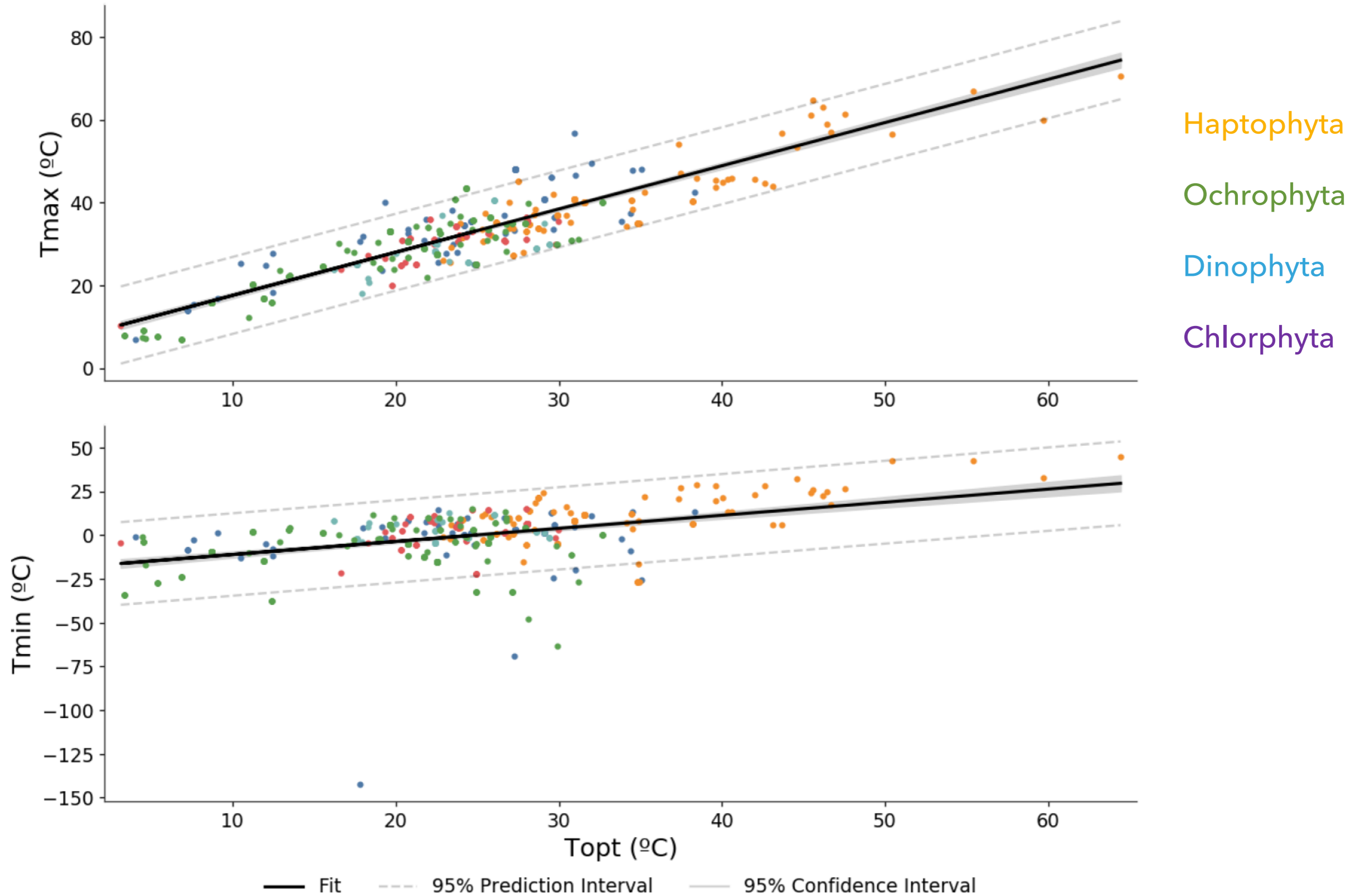


Océania

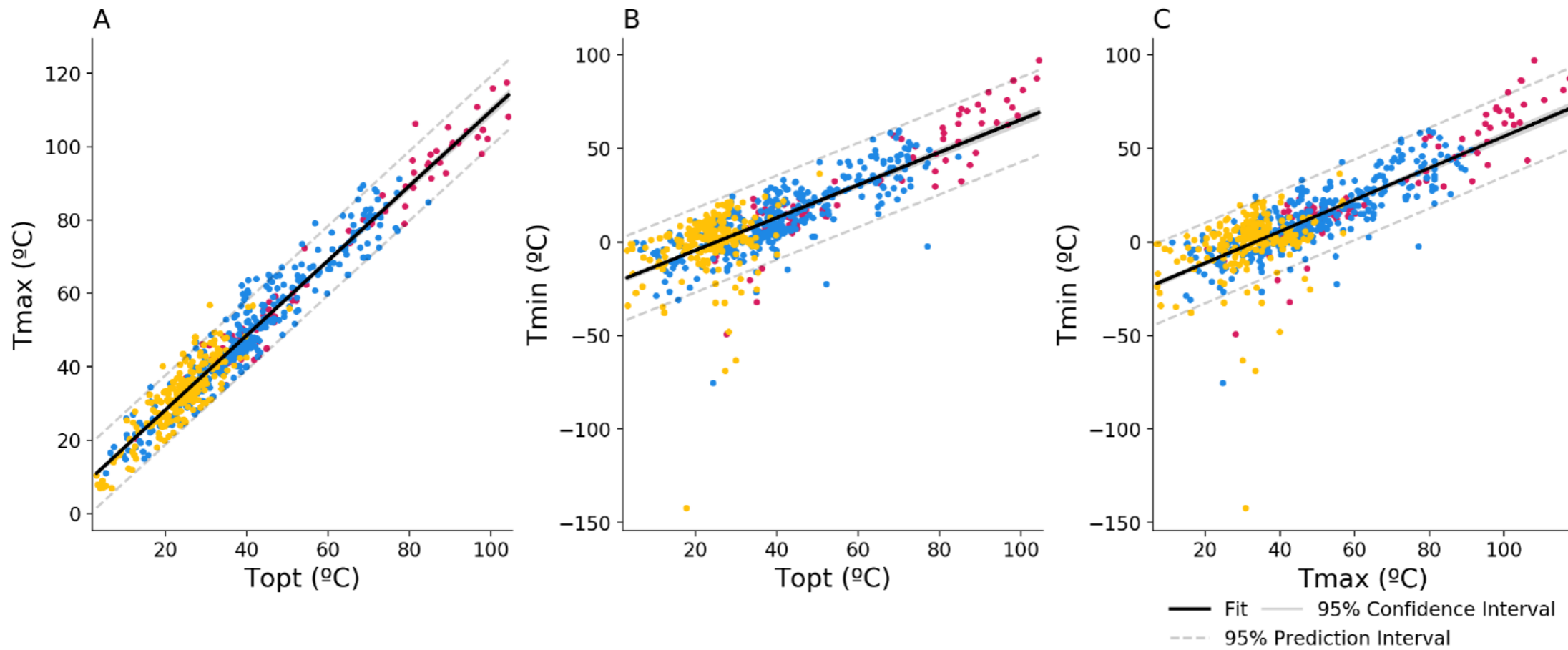
Relationship between cardinal parameters



Link between T_{min} , T_{max} and T_{opt}



Cardinal temperature links among microorganisms



Eukayota

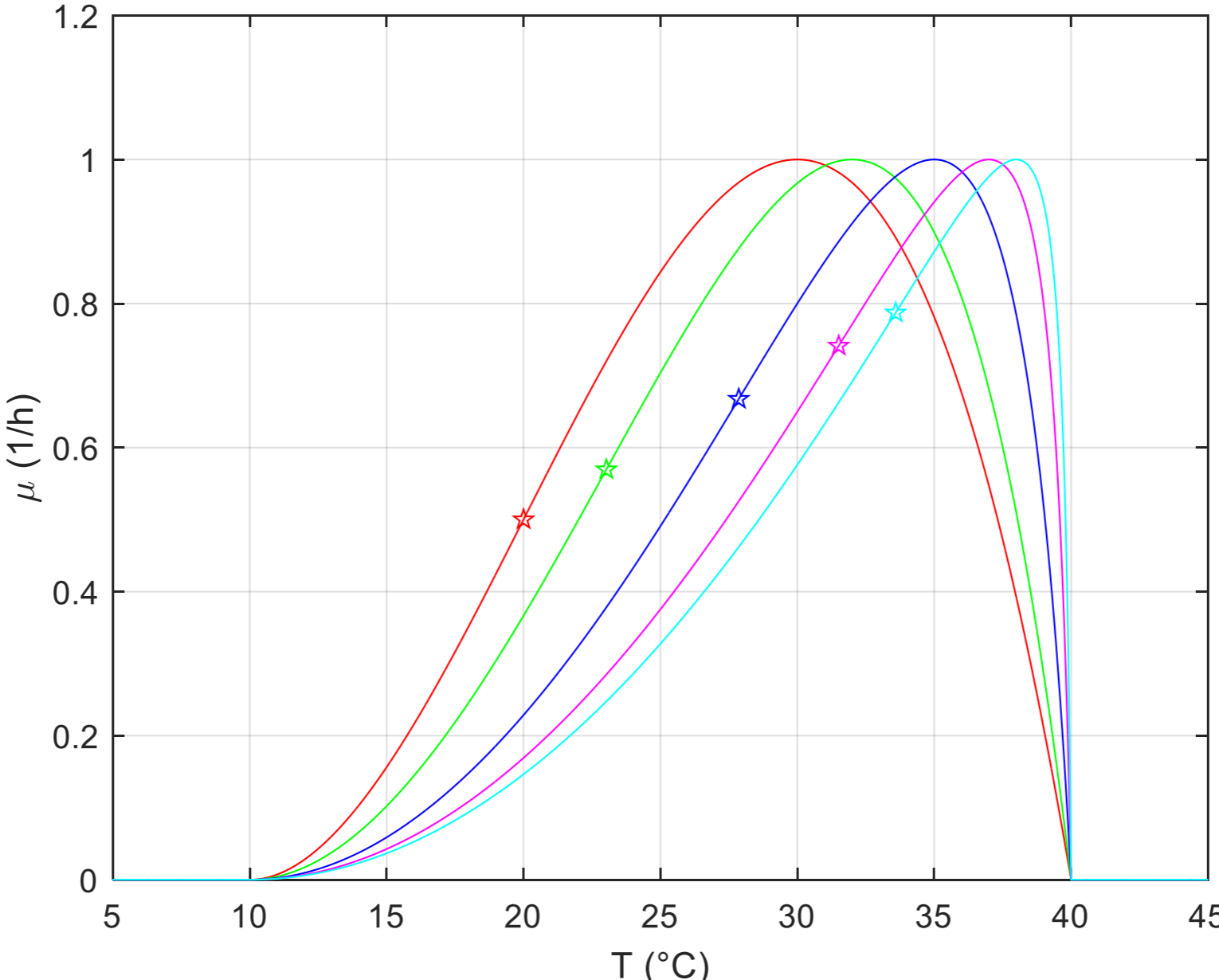
Bacteria

Archae

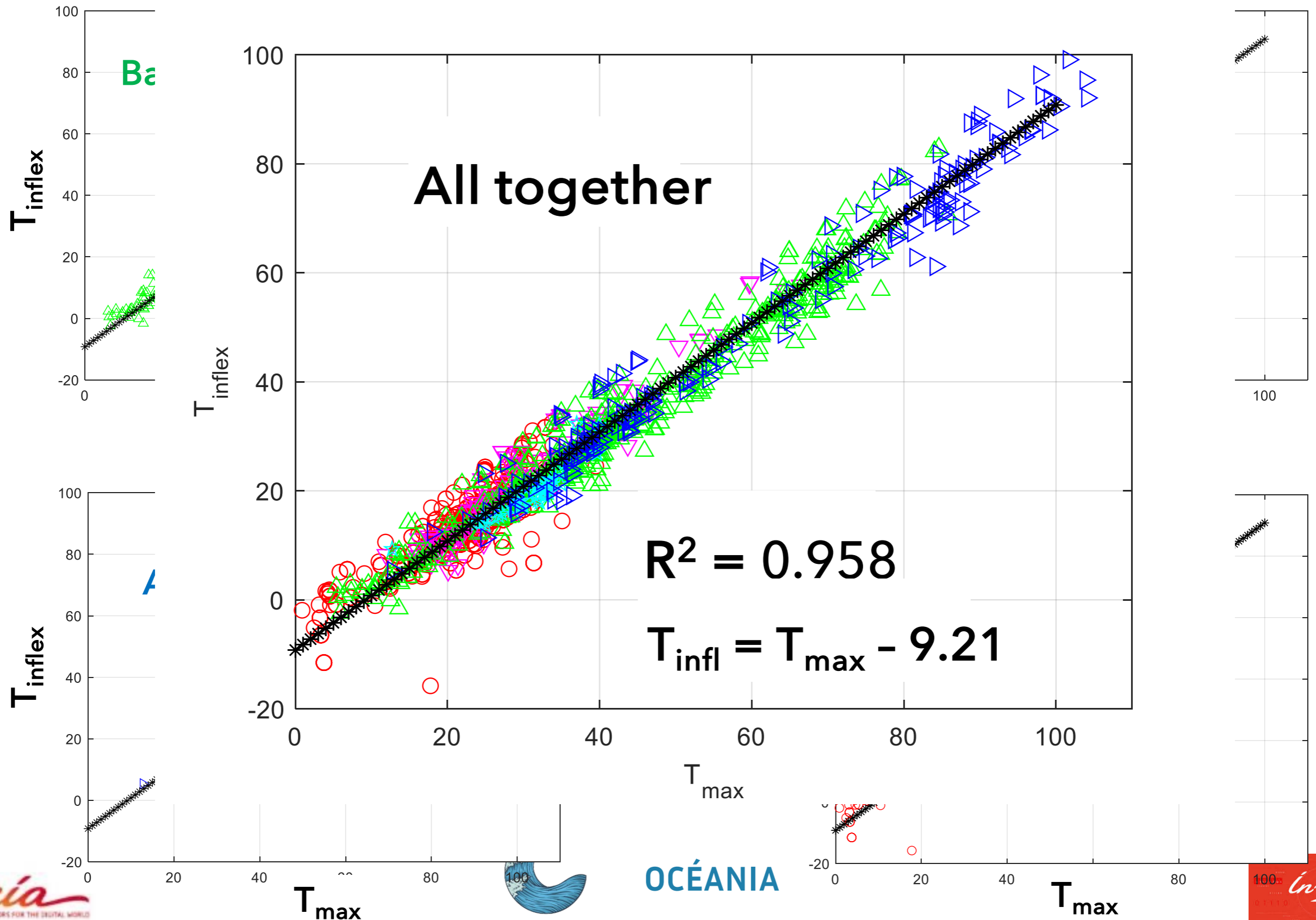


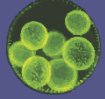
OCEANIA

Which of these growth curves is realistic?



There is a link with the inflexion point!

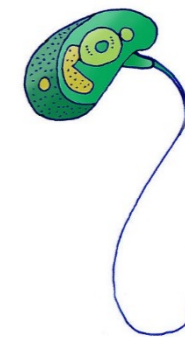
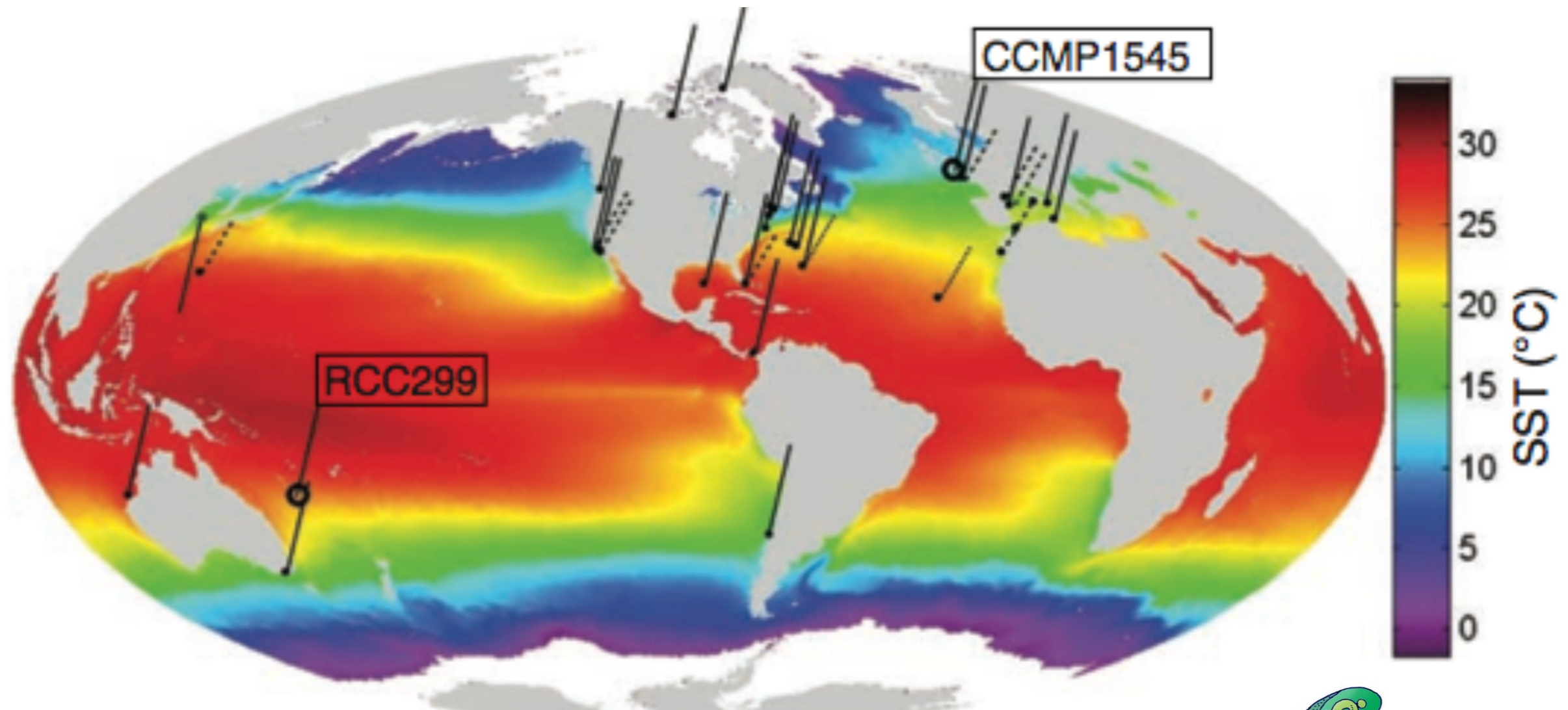




LINK BETWEEN LOCAL ENVIRONMENT AND TEMPERATURE RESPONSE



Micromonas temperature response in present and future oceans



Micromonas: **pico eucaryote**
(Mamiellaceae)



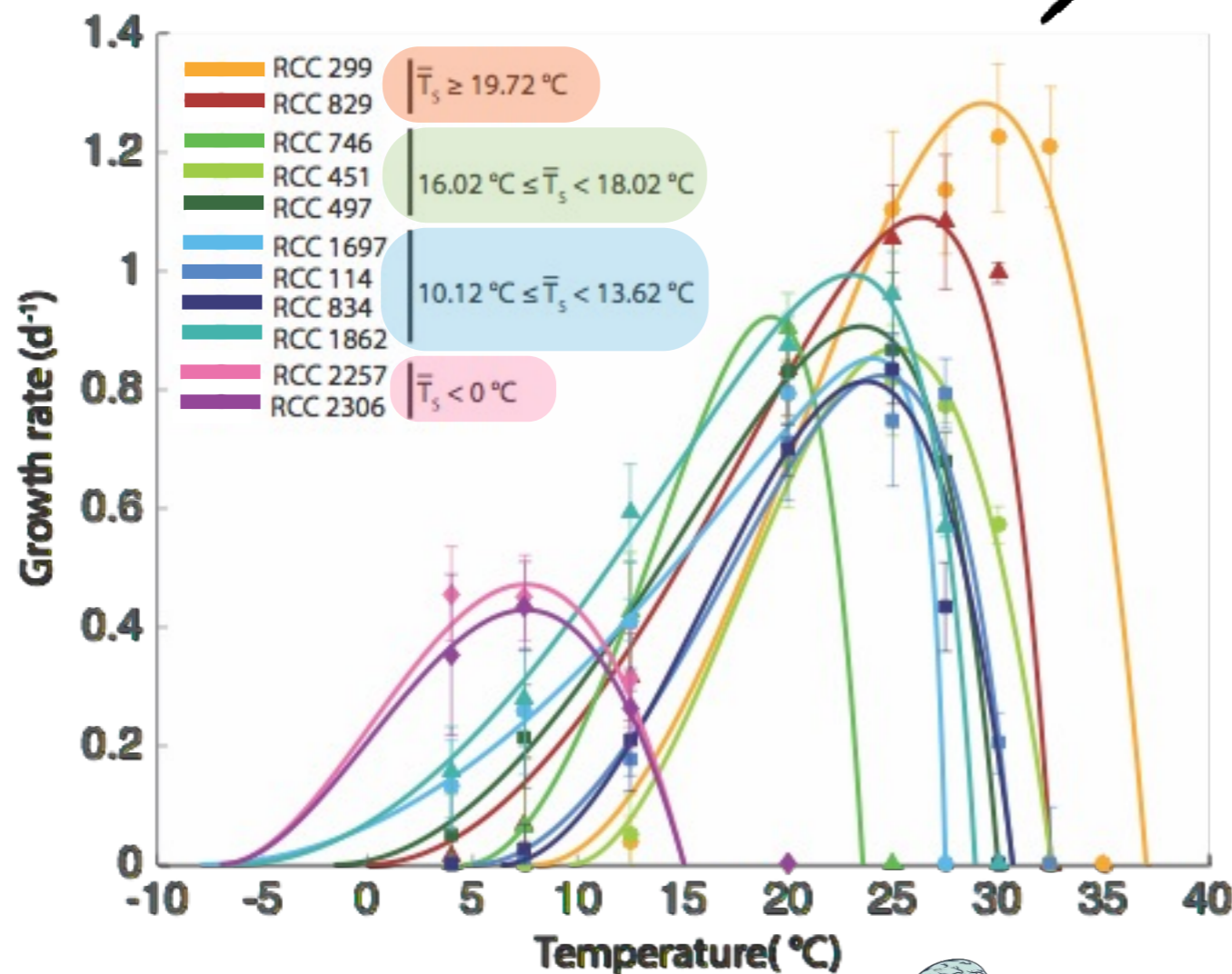
Link environment with thermal response

➔ Thermal response

11 *Micromonas* strains

BR model

Thermal response data base



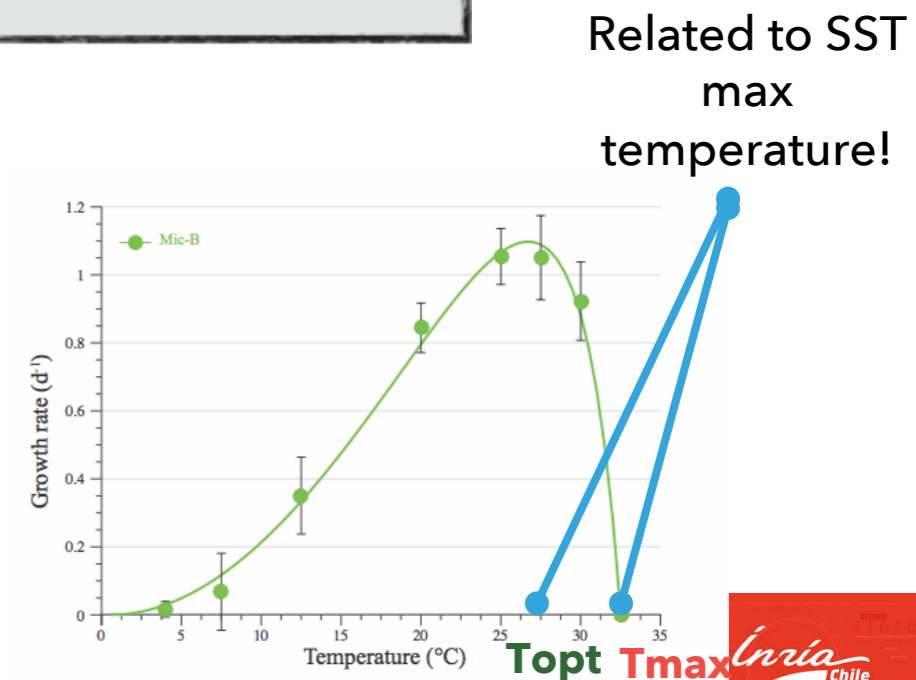
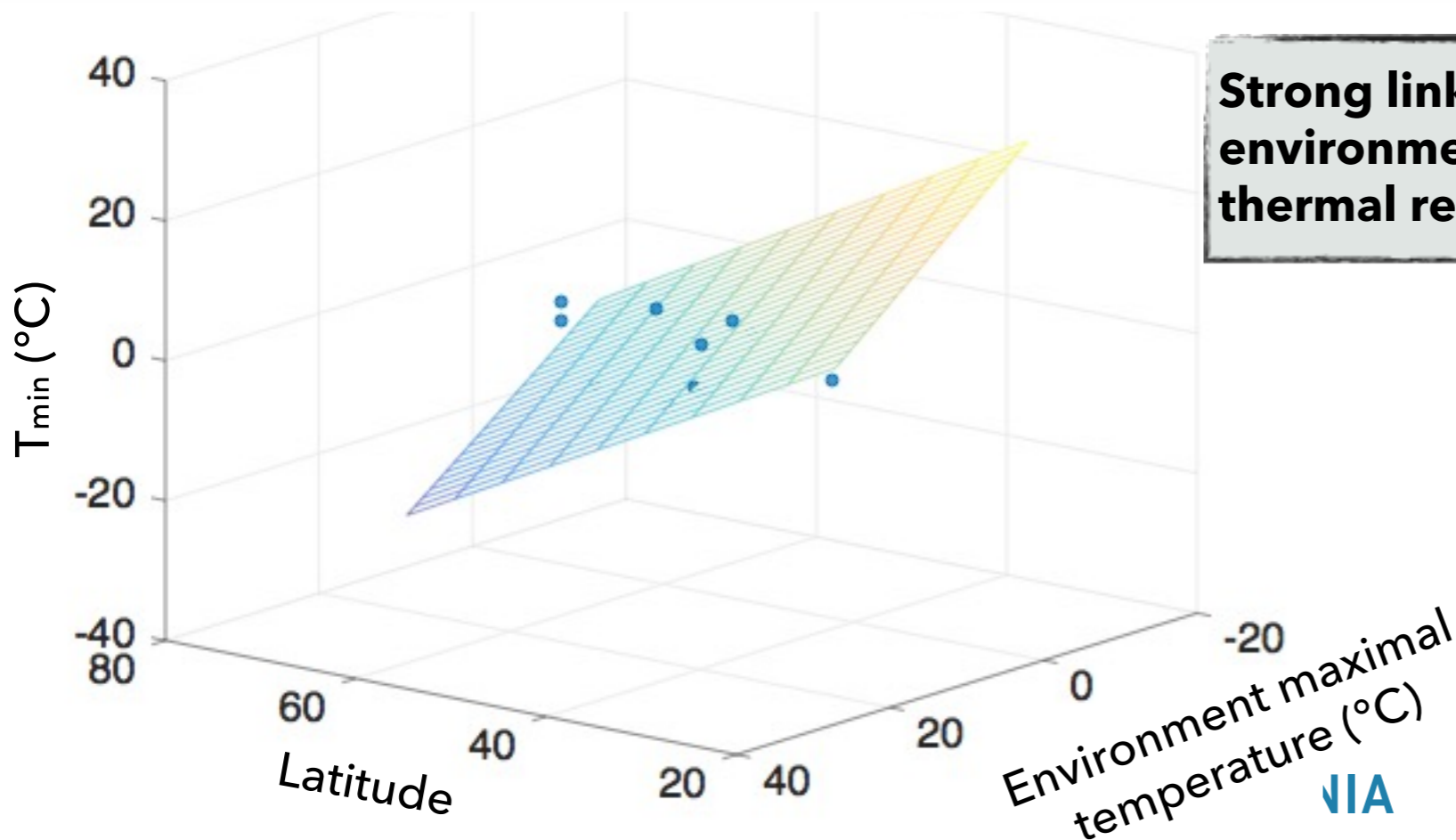
Strains	°C			d ⁻¹
	Tmin	Topt	Tmax	muopt
RCC299	7.94	29.29	37.05	1.28
RCC829	-0.08	26.33	32.51	1.09
RCC746	4.60	19.18	23.57	0.92
RCC451	9.59	25.13	32.56	0.87
RCC497	-1.59	23.51	30.00	0.91
RCC1697	-16.04	24.04	27.5	0.85
RCC114	1.01	24.49	30.68	0.82
RCC834	6.34	23.71	30.71	0.81
RCC1862	-11.64	23.01	28.92	0.99
RCC2257	-14.12	7.03	16.91	0.45
RCC2306	-9.74	7.60	15.35	0.44

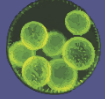
Link environment with thermal response

➔ Linear model

Demory et al. 2019, 2021

Cardinal Parameter	Model	R ² adjusted	p-value
μ_{opt}	$\mu_{opt} = 0.03 \bar{T}_S + 0.47$	0.90	$5.68 \cdot 10^{-6}$
T_{max}	$T_{max} = 0.73 T_S^+ + 14.46$	0.84	$4.29 \cdot 10^{-5}$
T_{opt}	$T_{opt} = 0.81 T_S^+ + 6.5642$	0.85	$3.22 \cdot 10^{-5}$
T_{min}	$T_{min} = -0.76 Lat - 0.92 \bar{T}_S + 49.33$	0.47	0.03

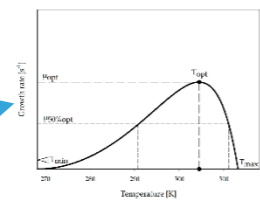
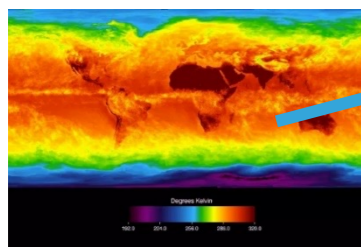




CAN WE PREDICT PHYTOPLANKTON BIODIVERSITY FROM SST?



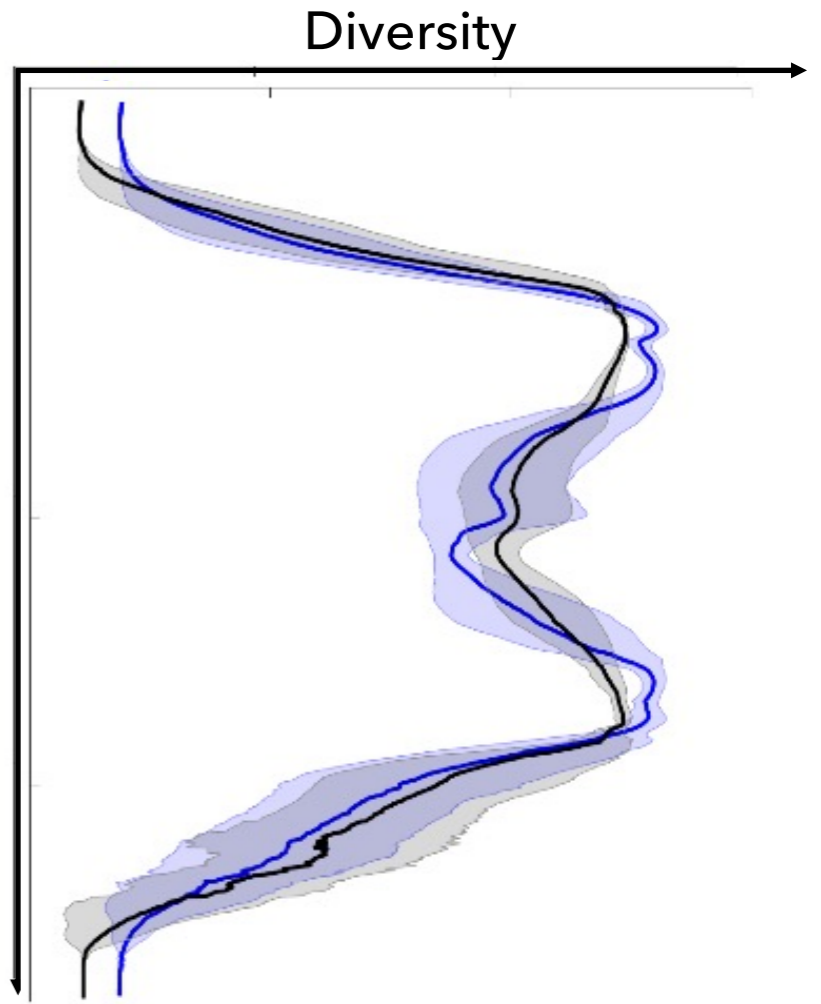
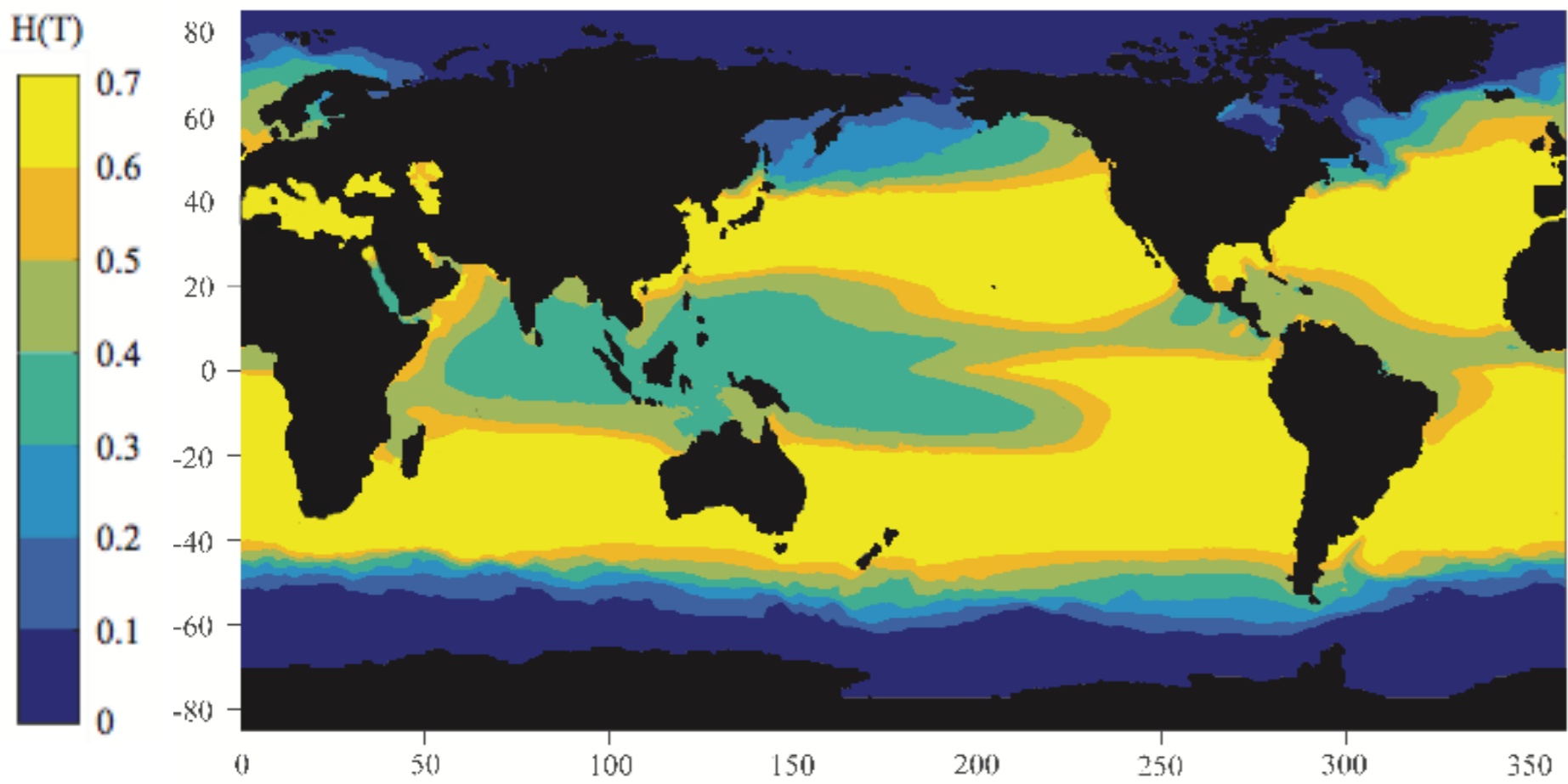
Predicting micromonas diversity response to temperature = representative of phytoplankton

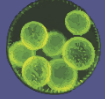


Micromonas: a phytoplankton sentinel

— Phytoplankton Diversity from Thomas *et al.* 2012
 — Micromonas Diversity

Average from 1993 to 2012





CAN WE PREDICT THE EVOLUTION OF THE TEMPERATURE RESPONSE?

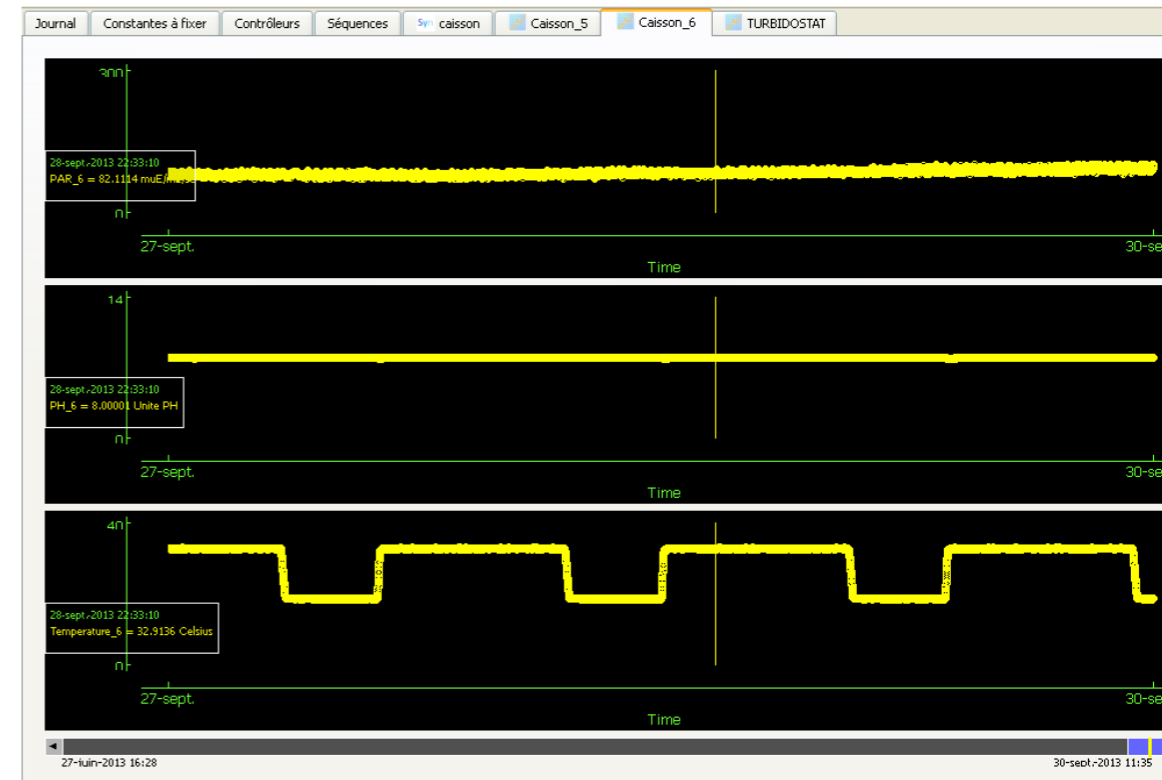
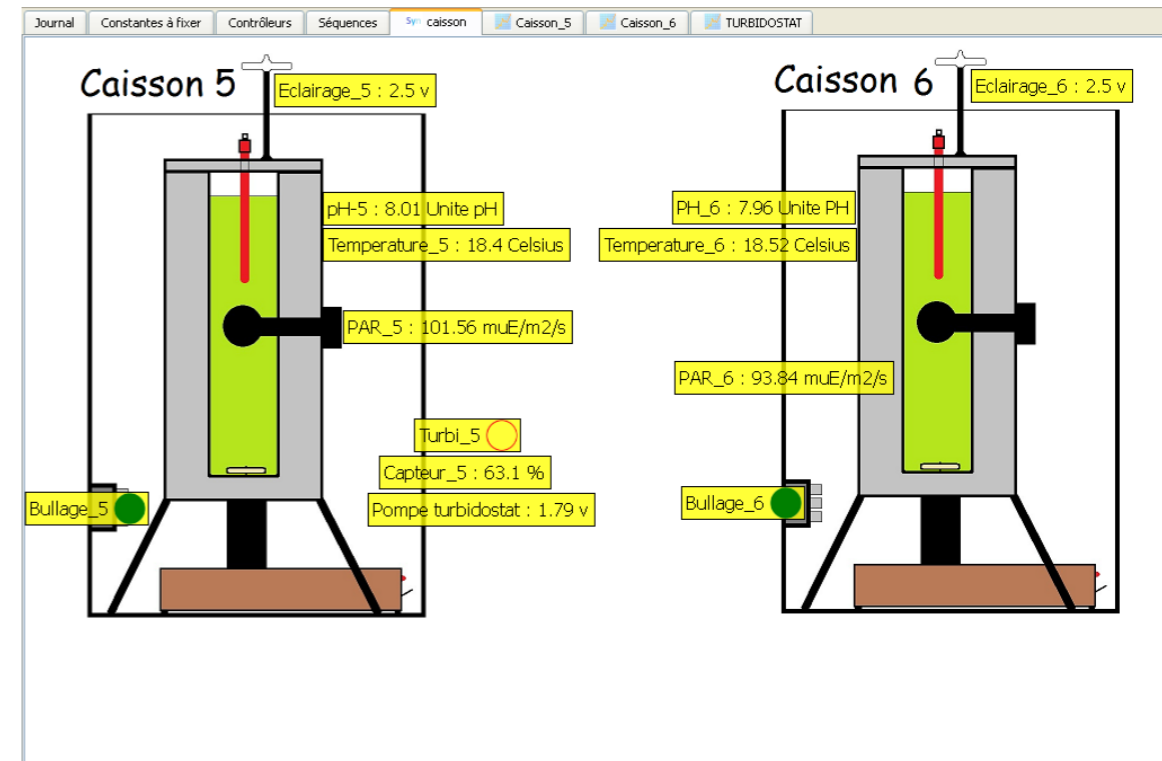


The selectiostat principle

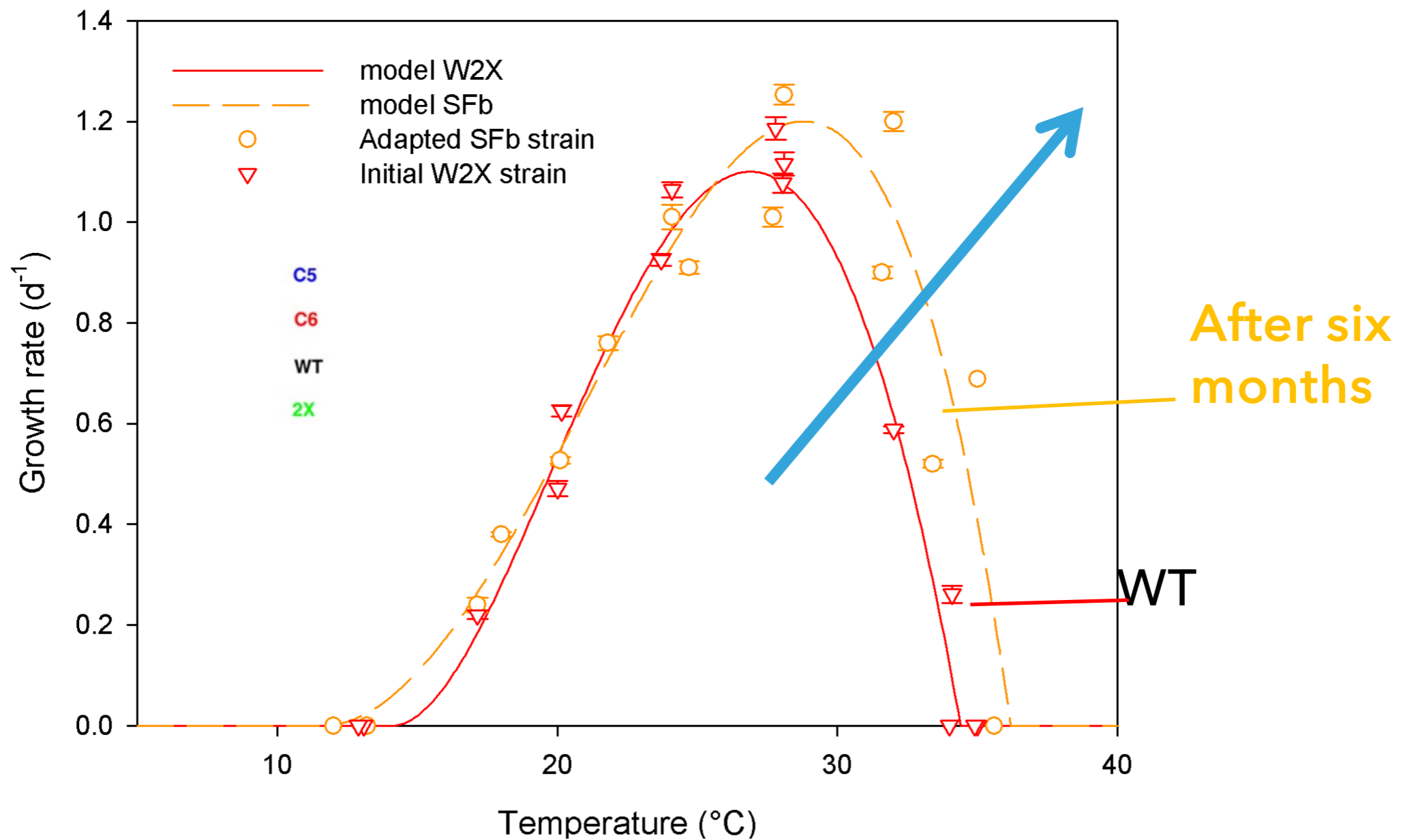
Computer controlled devices to trigger adaptation on the long term in a dynamical realistic environment



Designed by E. Pruvost



Temperature adaptation experiments



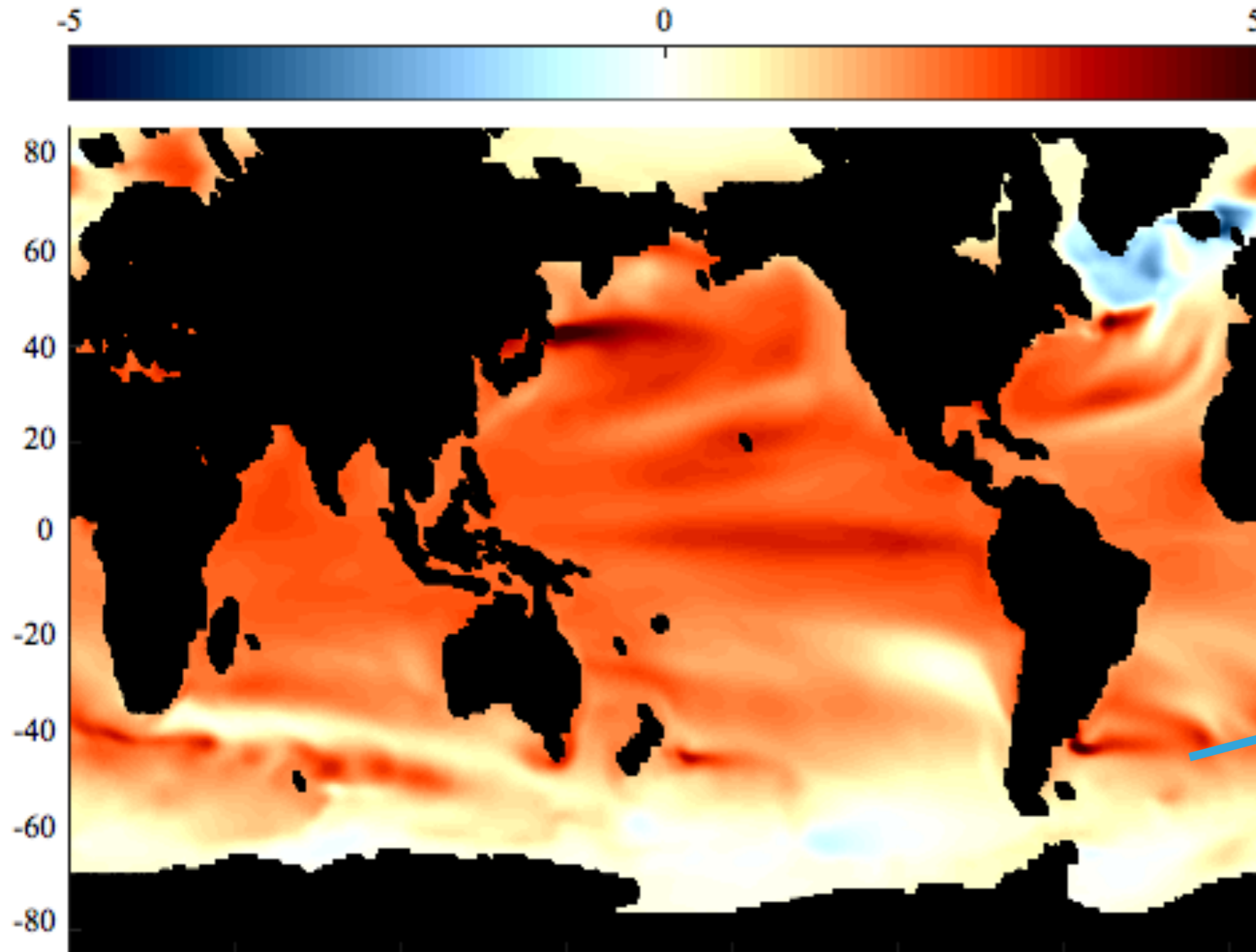
- Increase of max growth rate

- Increase of max temperature

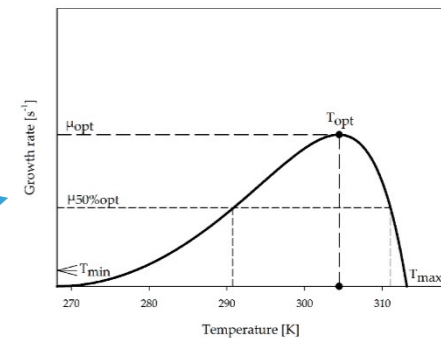
Bonnefond et al. 2017, Plos One

Evolution of ocean temperature

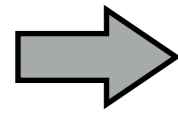
➔ SST anomalies (2001 – 2100)



Global warming

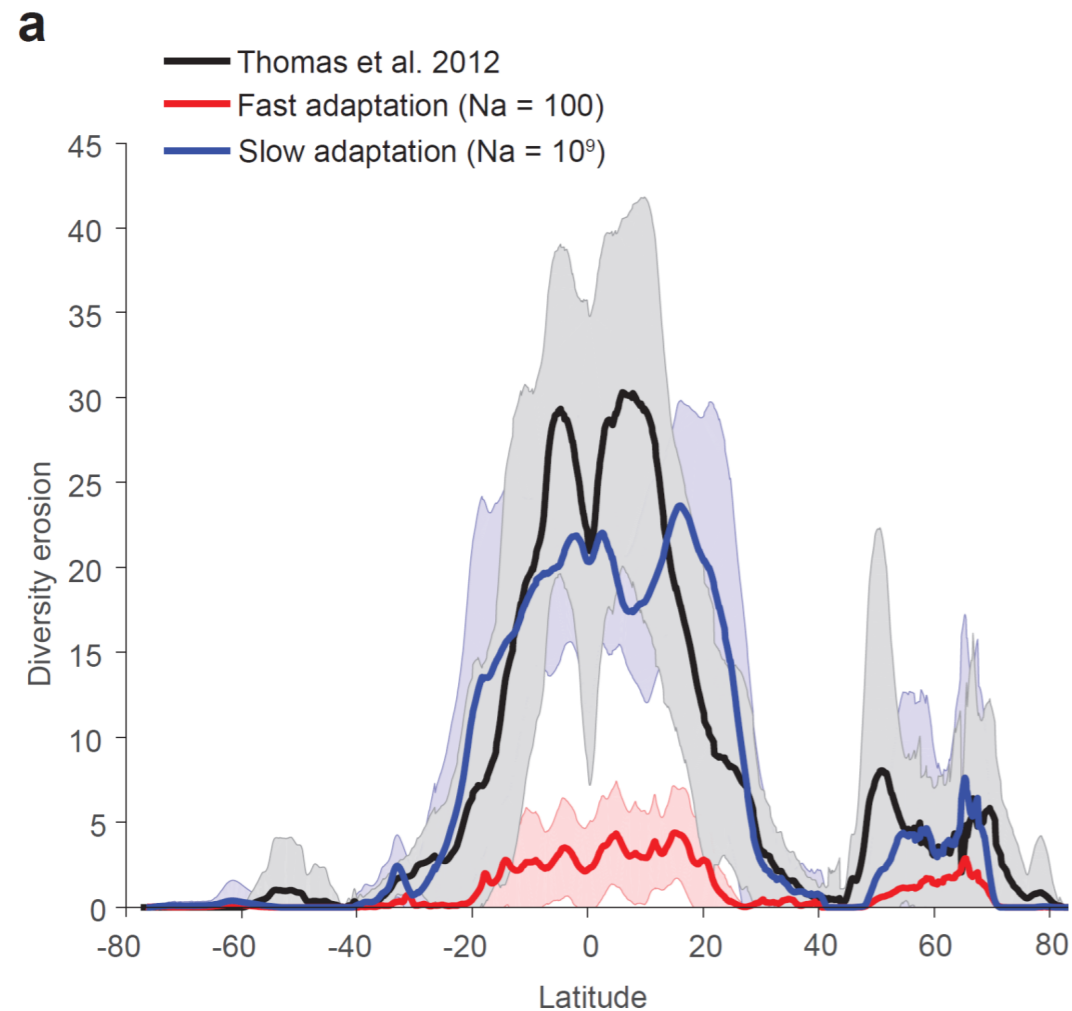


How fast can phytoplankton adapt?



Importance of the adaptation time scale

Phytoplankton from Thomas *et al.* 2012



- Temperature plays a key role (as light) on phytoplankton: but it has not been studied and understood with the same details!
- Much remains to be done to understand and represent in models acclimation to temperature
- Understand and include adaptation to temperature change in the models
- Key question to predict the impact of global changes!

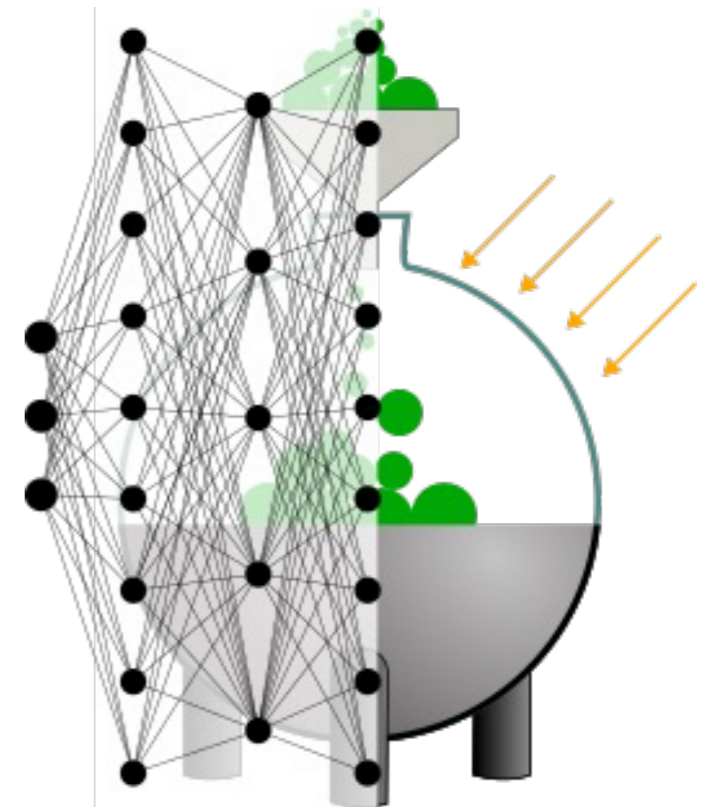


- Understanding the rules driving response to temperature in phytoplankton (O. Bernard)
- **Neural ODE for representing phytoplankton growth driven by light (I. Fierro)**
- Towards hybrid modelling of artificial microbial ecosystems (F. Casagli)
- Spatio-temporal high-resolution models of particulate organic matter abundance in the ocean (R. Ranini)

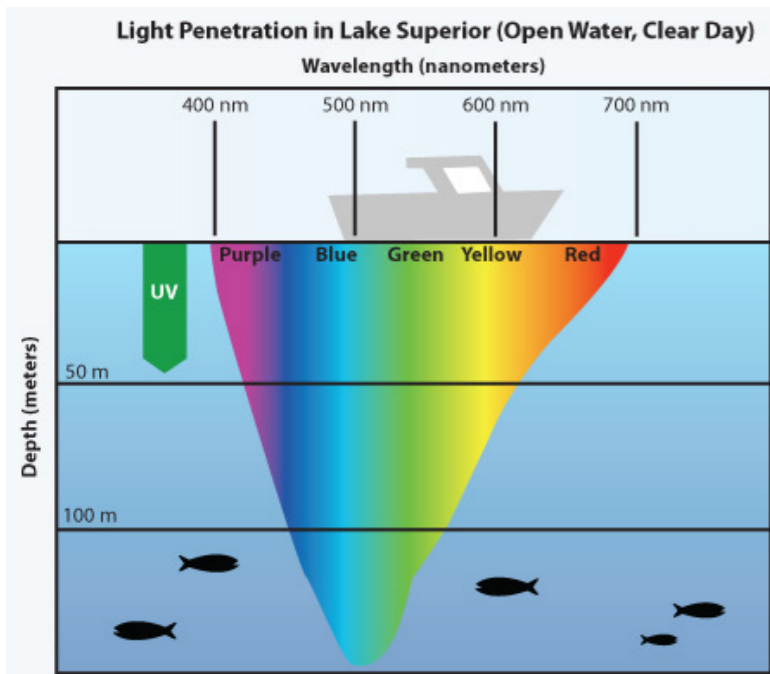
NEURAL ODES FOR PHYTOPLANKTON MODELING

Combining first order principles
and neural networks

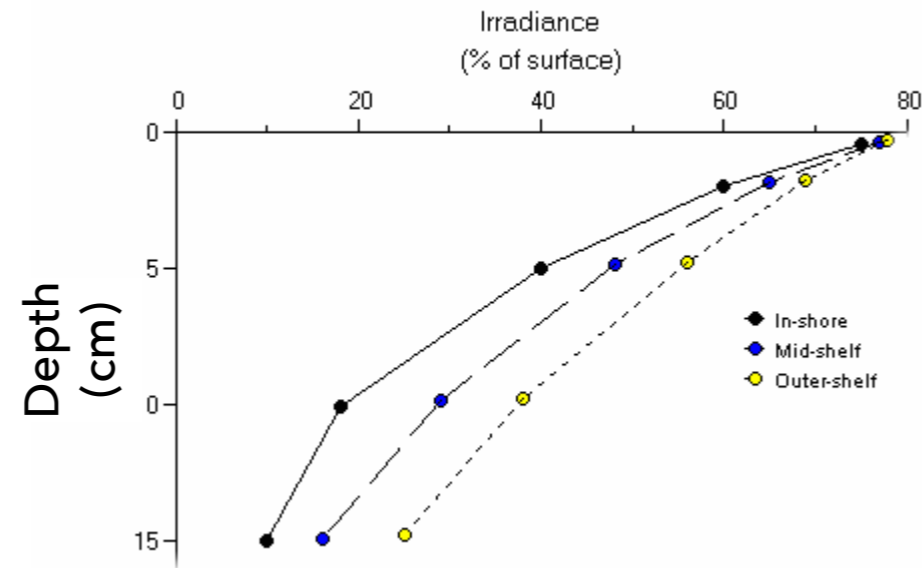
J. Ignacio Fierro U. & Olivier Bernard



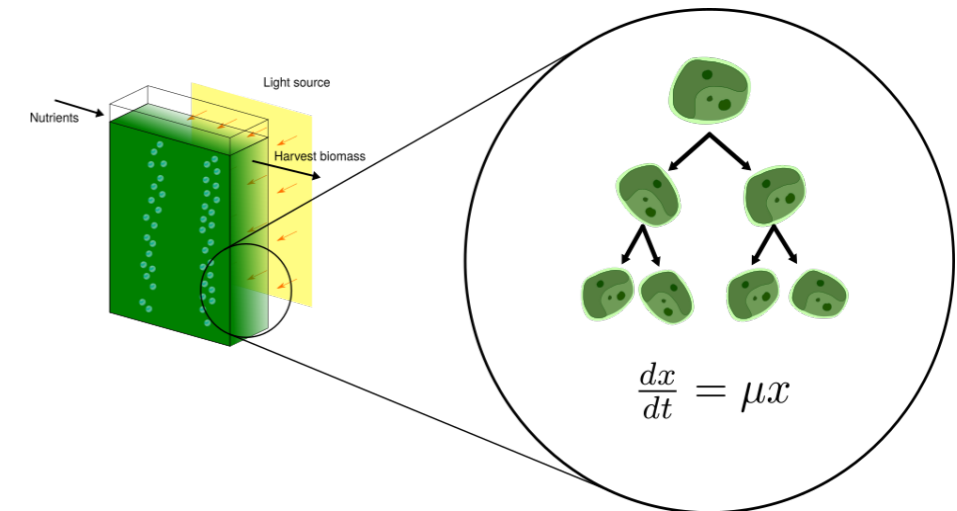
Modeling phytoplankton evolution in a light gradient



Ocean



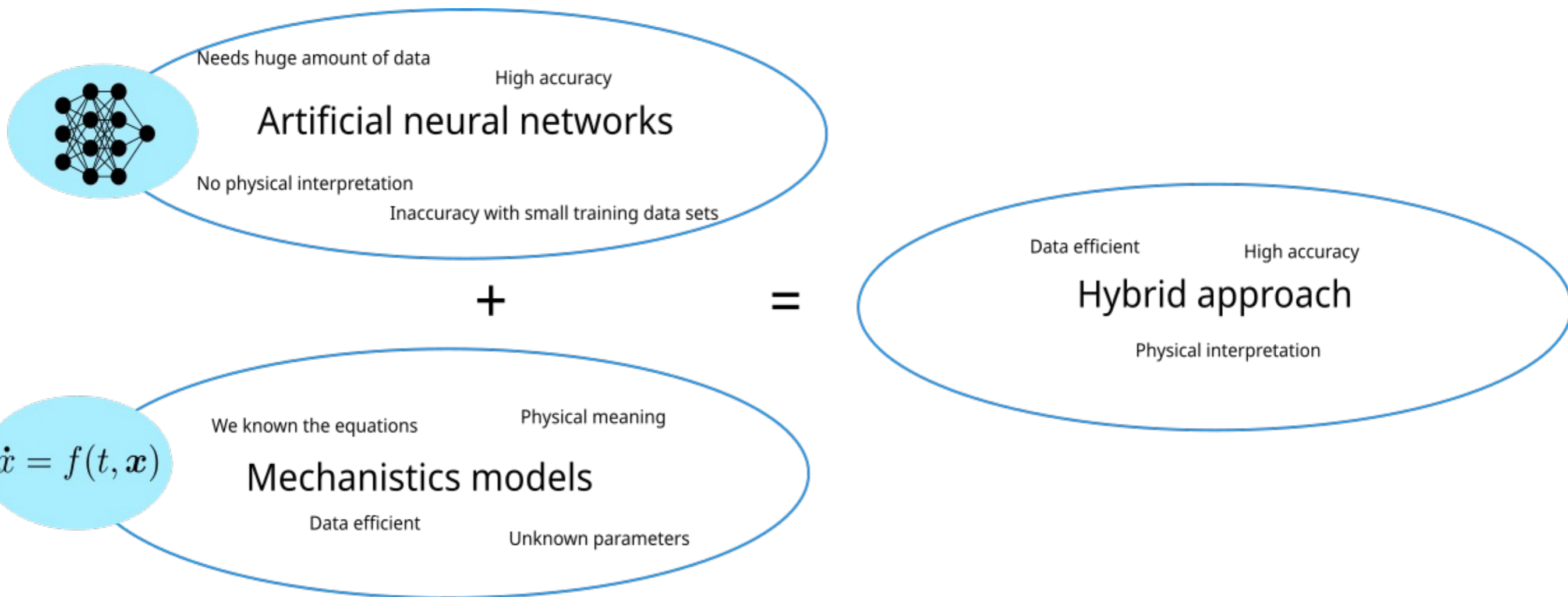
Light availability



Photobioreactors

Growth rate is affected by: Temperature, pH, nutrients, **light**, etc.

Neural Ordinary Differential Equations



Diatoms growing in photobioreactor

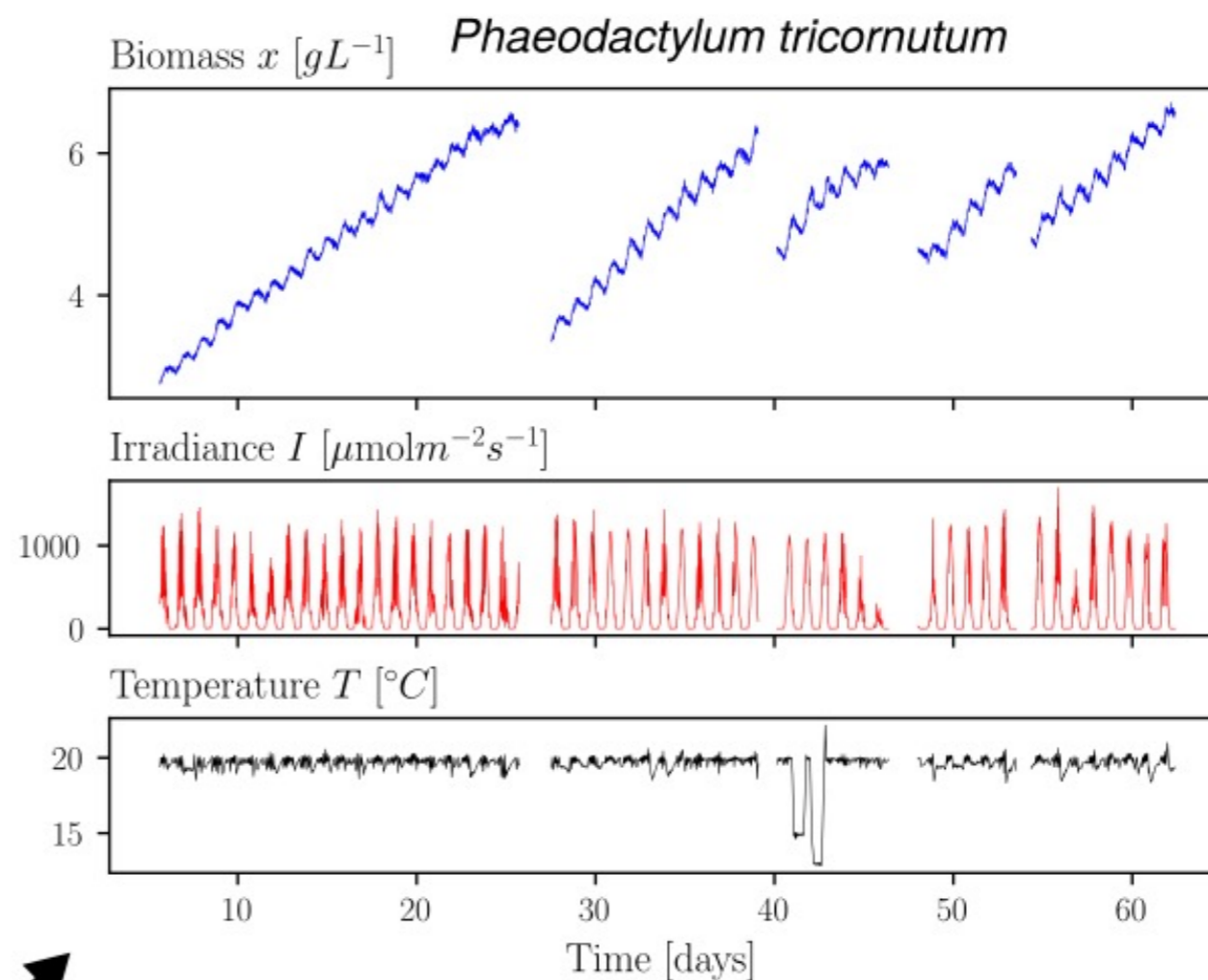


Phaeodactylum tricornutum cultivated under natural light in a 180L flat-panel airlift in a greenhouse (Leuna, Germany, July - September 2015).

Online measurements recorded every 10 minutes.

Fraunhofer Center for Chemical-Biotechnological Processes.

Diatoms growing in photobioreactor

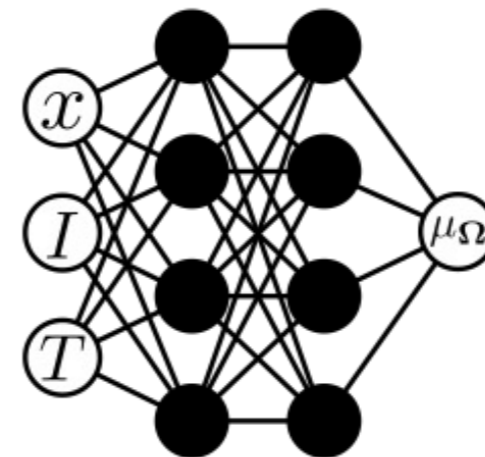
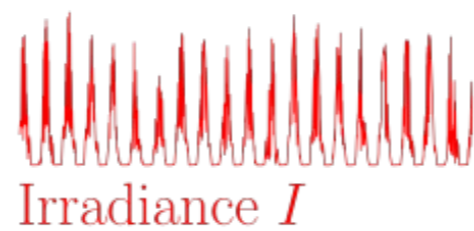
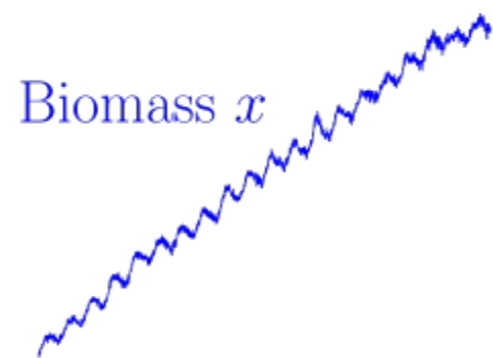


Online sensors

Neural ODE

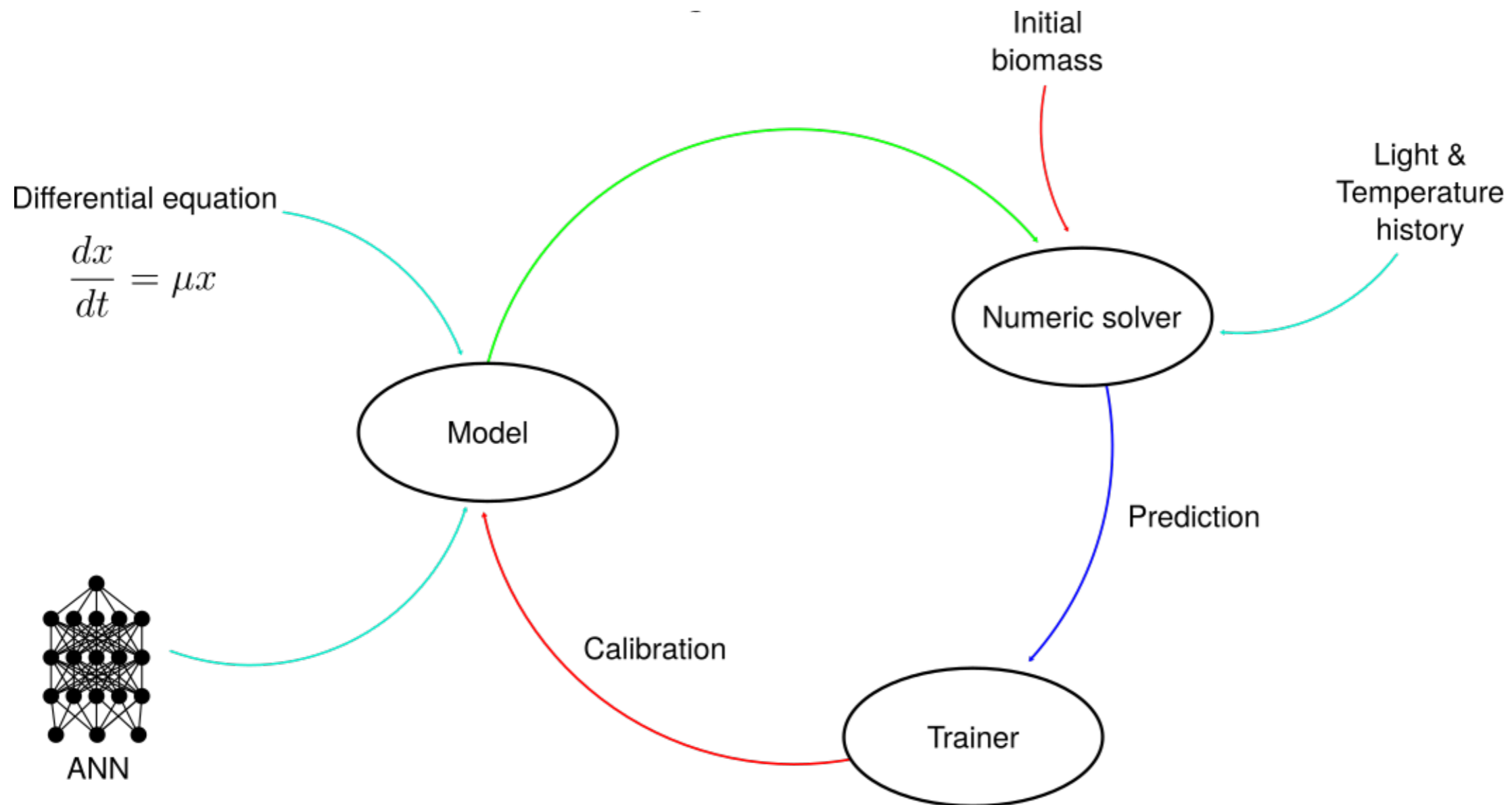


Online sensors



$$\frac{dx}{dt} = \mu_{\Omega}(x, I, T)x$$

Implementation of the model in PyTorch

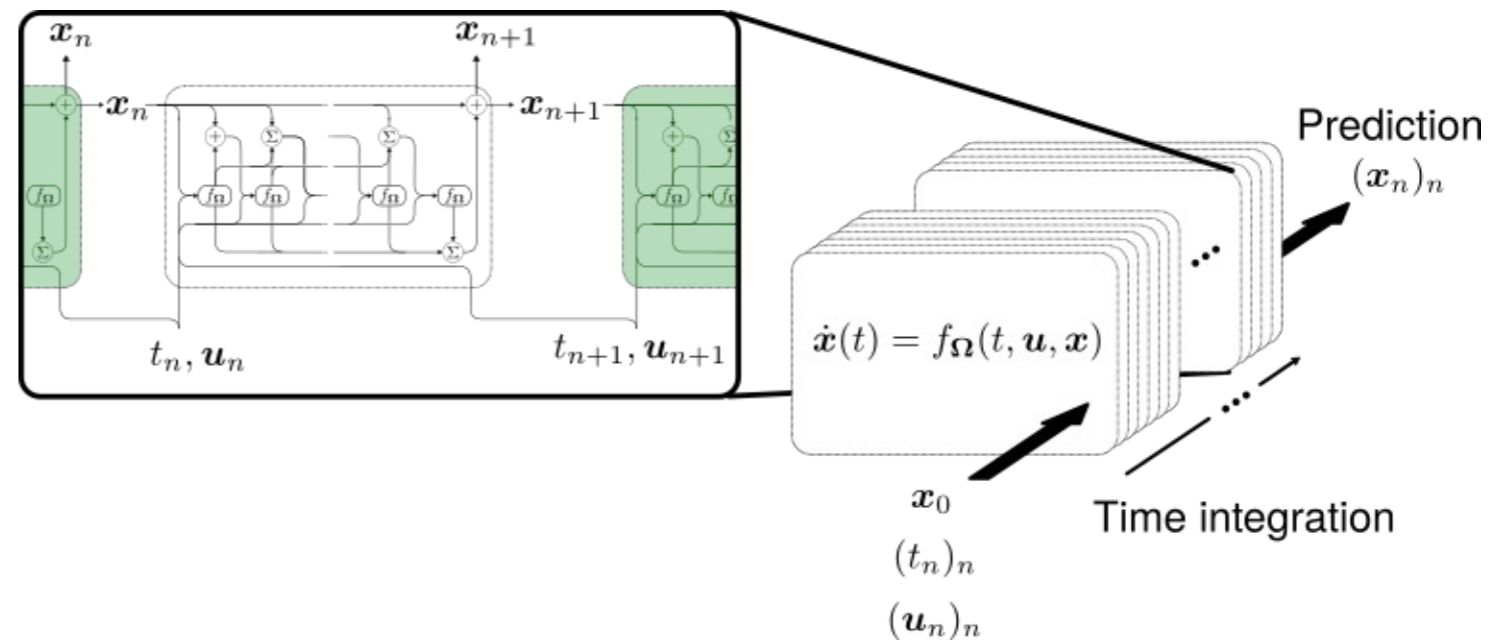


Numeric solver

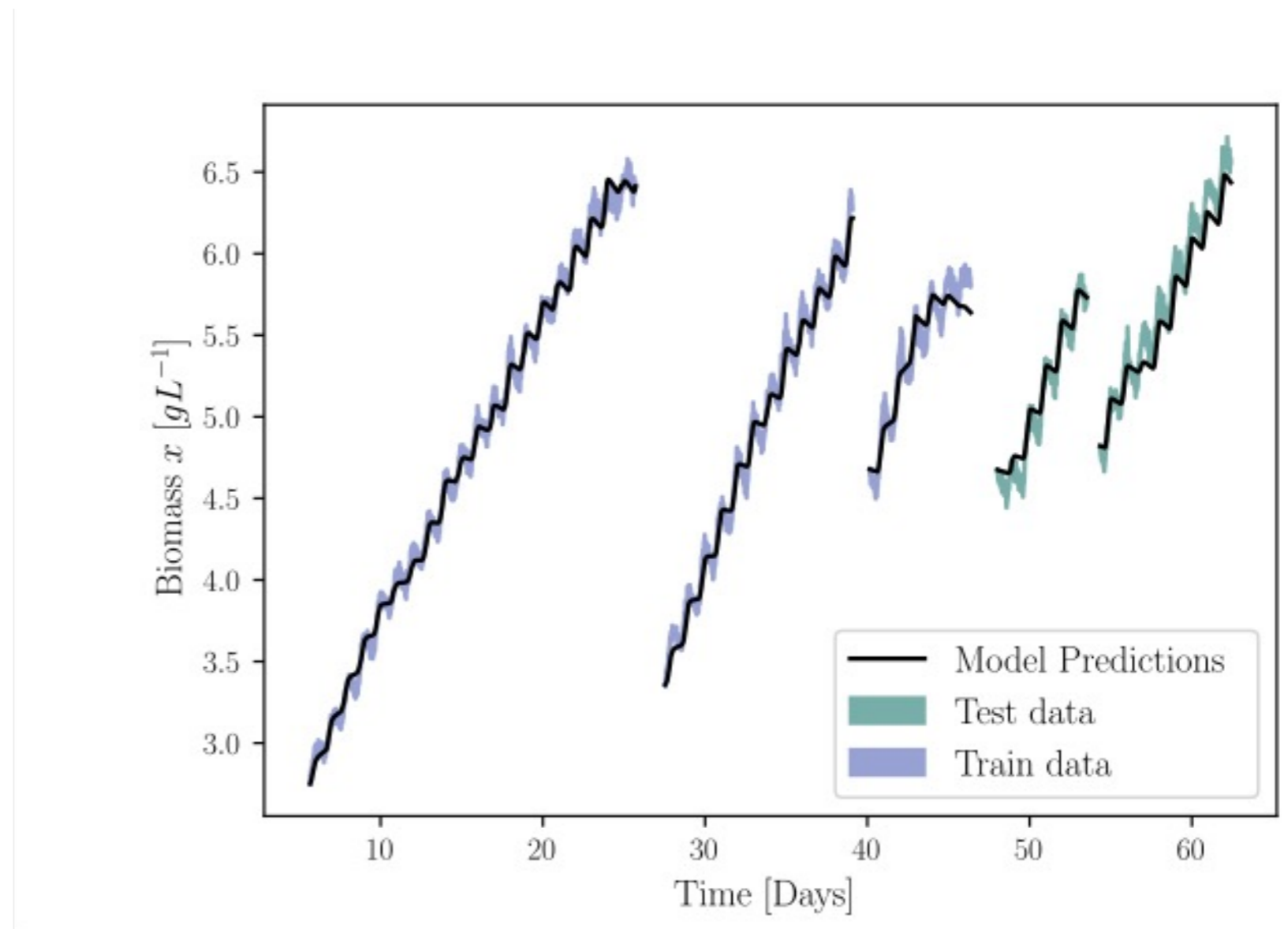
We code our own Runge-Kutta method as recurrent neural network to allow backpropagation.

Solving in batch: several equations can be solved at the same time.

Light and temperature are interpolated at the same time the equations are solved.



Results

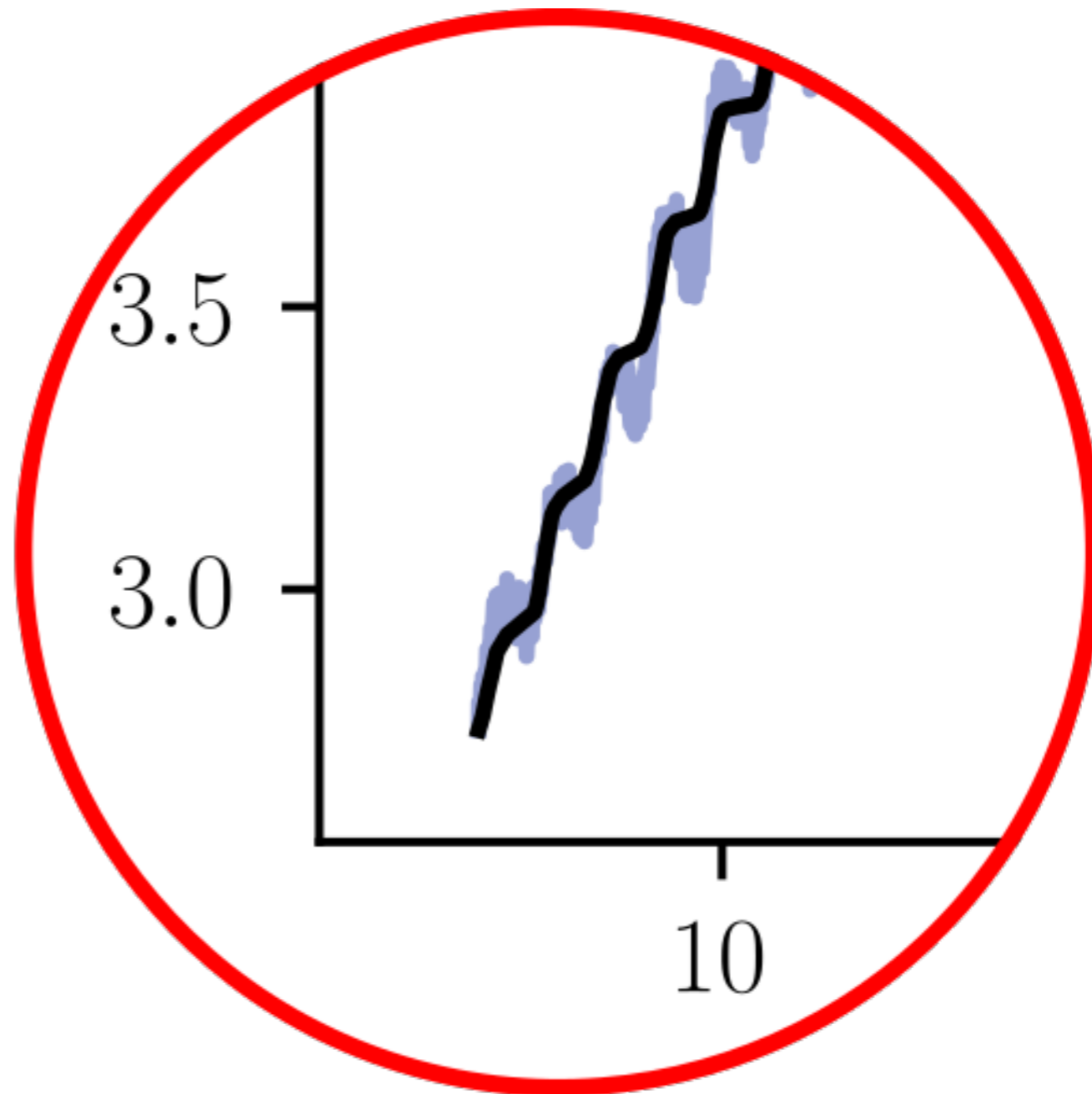


Low error

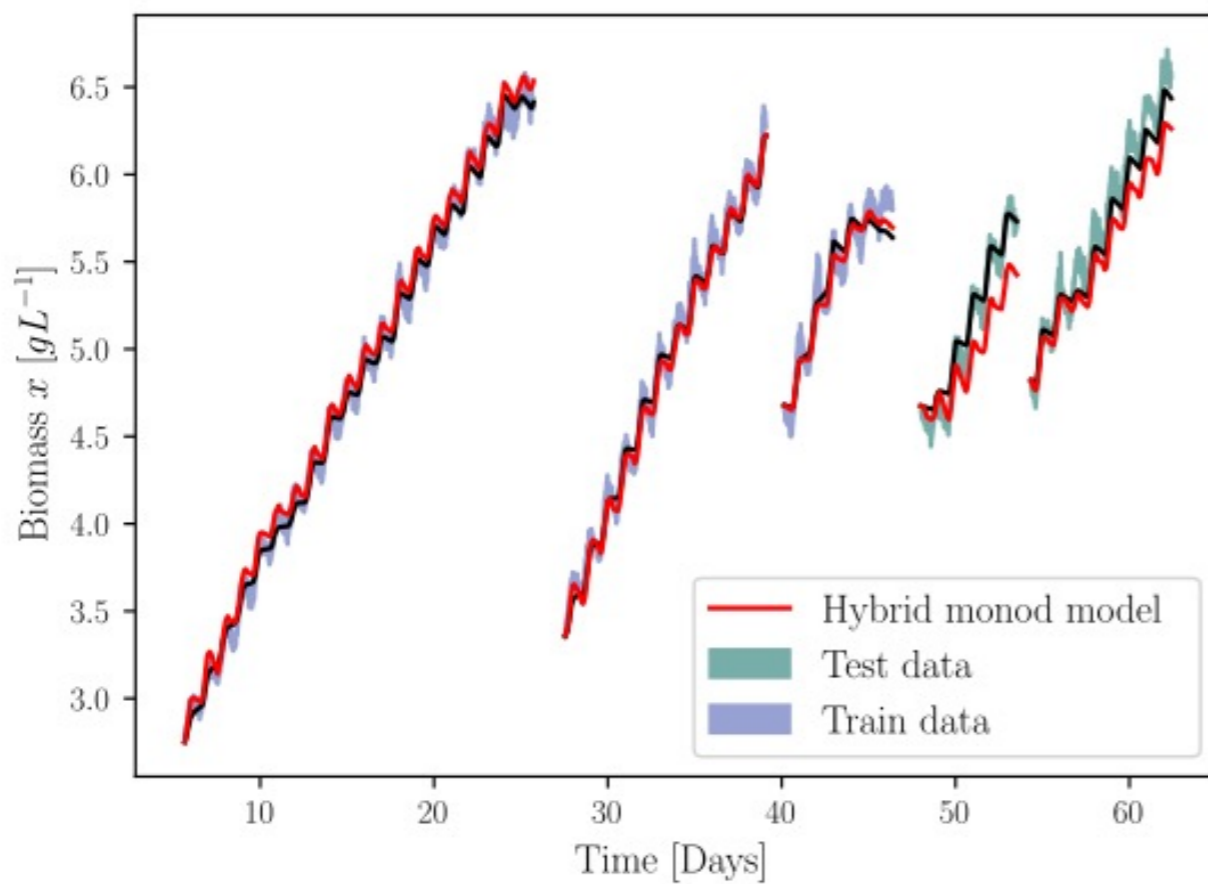
Error	Training dataset			Test dataset	
	Batch 1	Batch 2	Batch 3	Batch 4	Batch 5
RMSE	0.059	0.075	0.108	0.078	0.114
Percentage	1.037	1.318	1.648	1.247	1.697

Some Issues

Local inaccuracy



Solution: informed differential equation



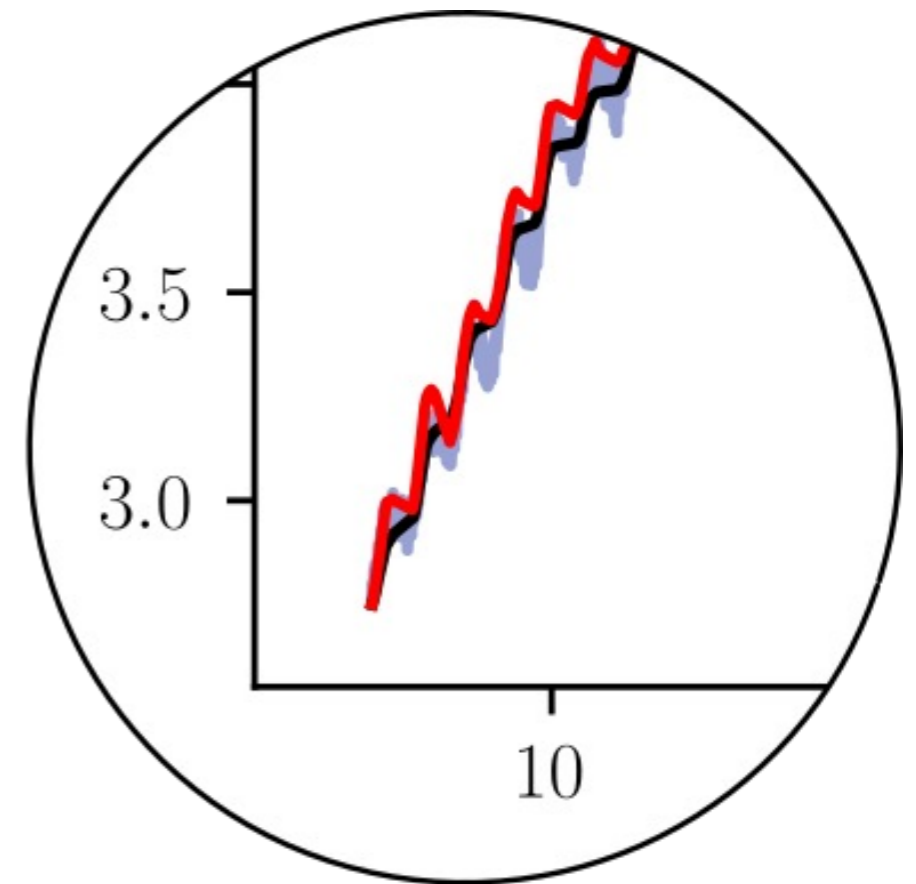
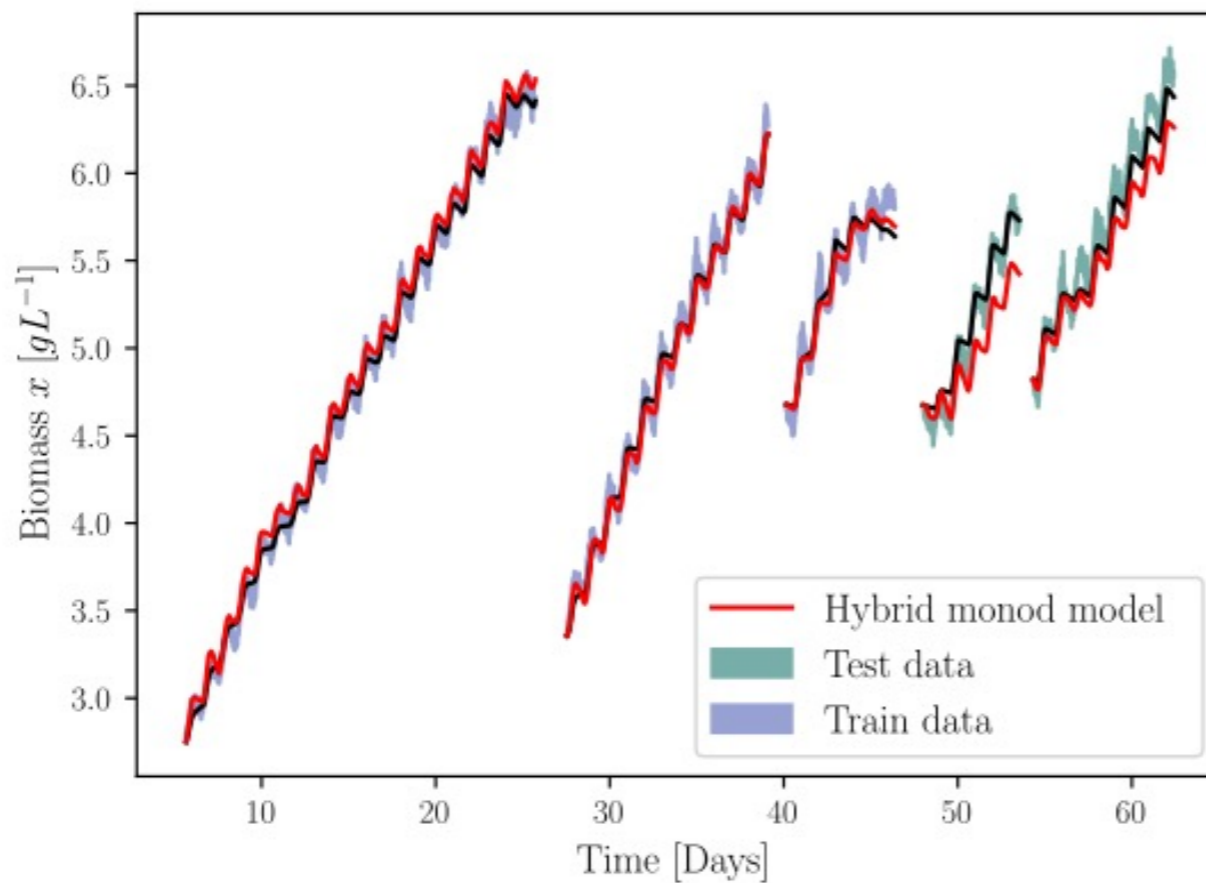
$$\frac{dx}{dt} = \frac{\mu_{\max}}{kx^b L} \ln \left(\frac{I + K_I}{Ie^{-kx^b L} + K_I} \right) x - Rx + NN_{\theta}(I, T, x)$$

↑ Monod kinetics
 +
 Beer - Lambert law

↑ Respiration rate

↑ Neural Network

Solution: informed differential equation



- Understanding the rules driving response to temperature in phytoplankton (O. Bernard)
- Neural ODE for representing phytoplankton growth driven by light (I. Fierro)
- **Towards hybrid modelling of artificial microbial ecosystems (F. Casagli)**
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FROM MECHANISTIC TO HYBRID MODELLING OF ALGAE-BACTERIA SYSTEMS

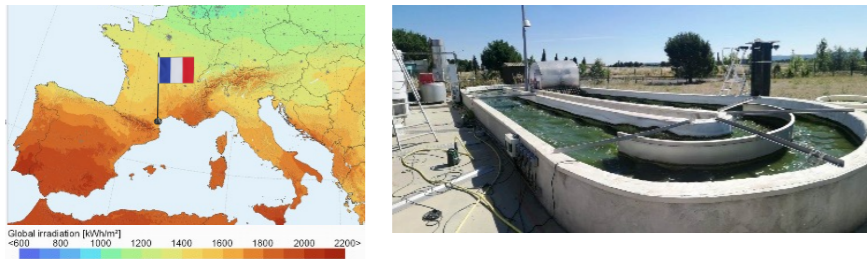
Francesca Casagli, Morgan Scalabrino, Joel Ignacio Fierro Ulloa, Olivier Bernard

Bi  CO₂re

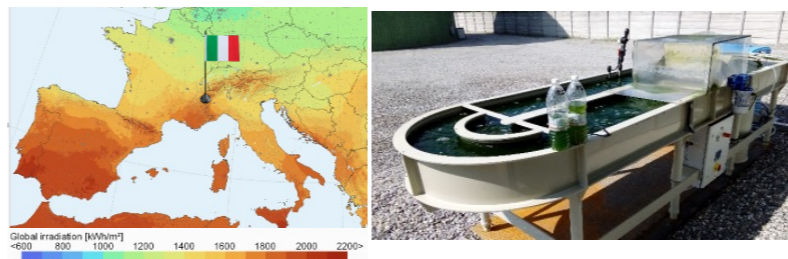
UNIVERSITÉ 
CÔTE D'AZUR

STARTING POINT: THE ALBA MODEL

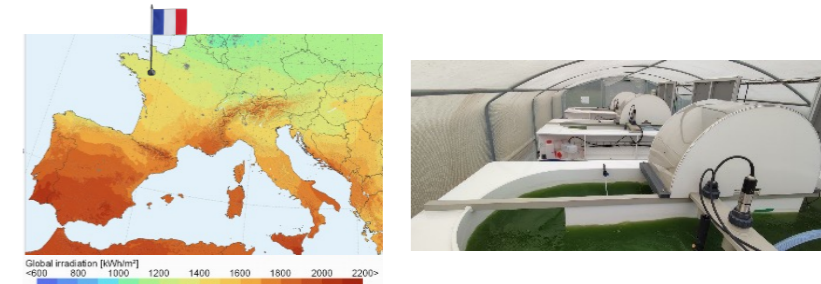
Narbonne



Milan



Rennes



Synthetic WW

443 days

CALIBRATION + VALIDATION

Piggery digestate

189 days

VALIDATION

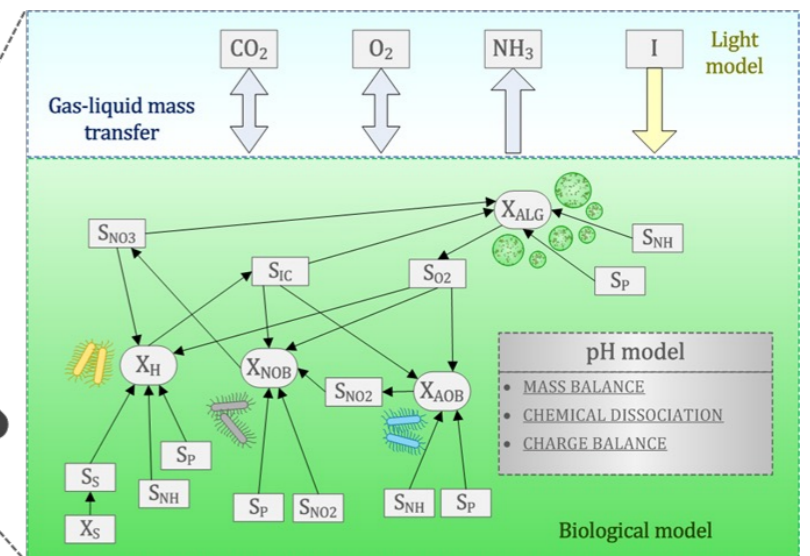
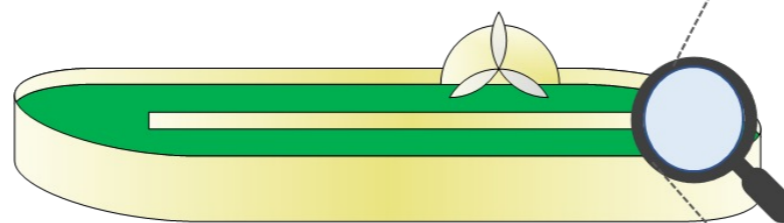
Piggery digestate

14 days

VALIDATION

$$\dot{\xi} = K \cdot \rho(\xi, T, \theta, \hat{H}^+) + \Delta(\xi, \xi_{in}, T, \hat{H}^+)$$

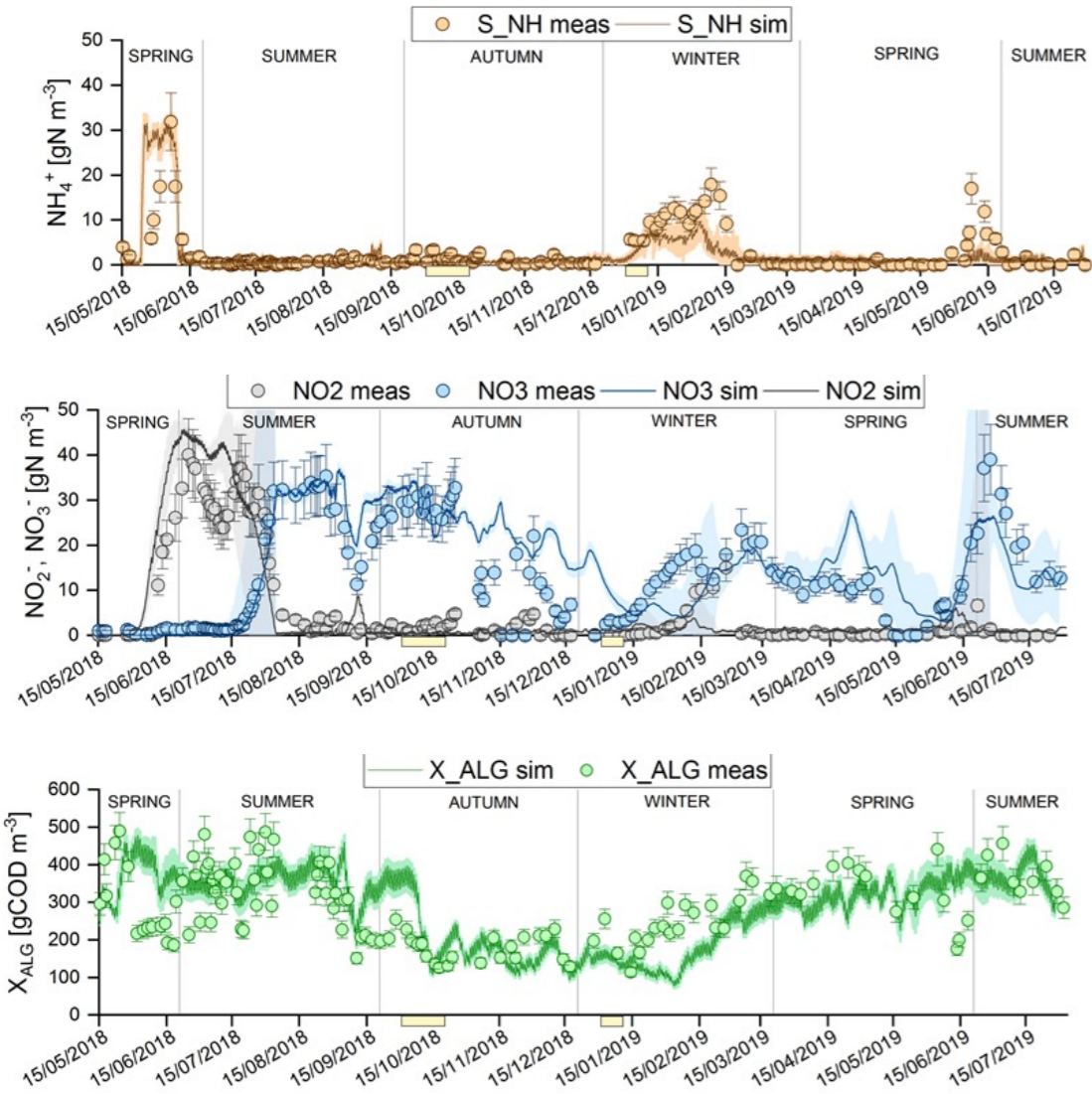
$$\dot{V} = Q_{in} - Q_{out} + Q_{rain} - Q_{evap}$$



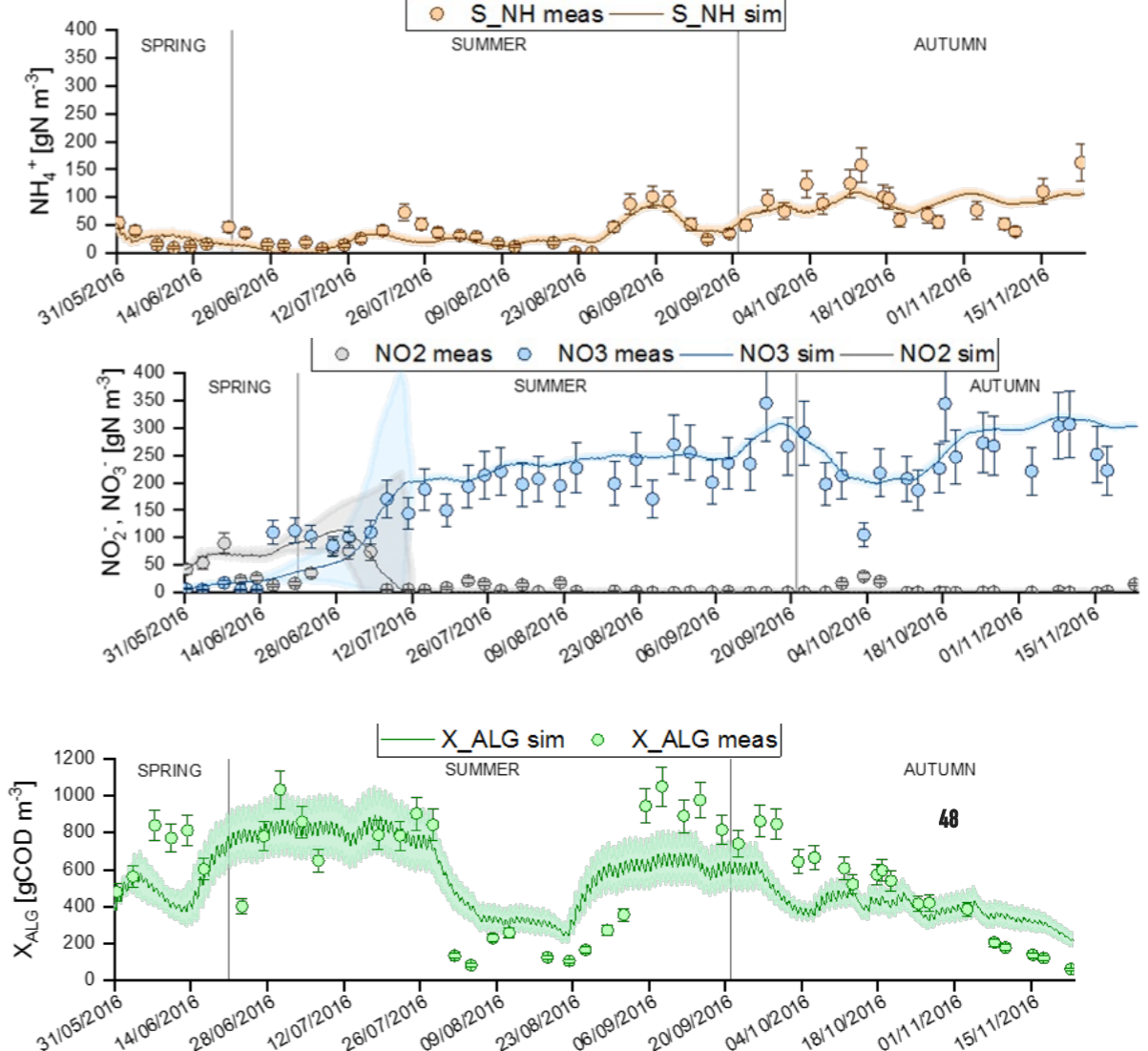
MECHANISTIC MODEL VALIDATION



Calibration - Validation



Validation



HYBRIDIZATION APPROACH: FROM MECHANISTIC MODELS TO PINNS

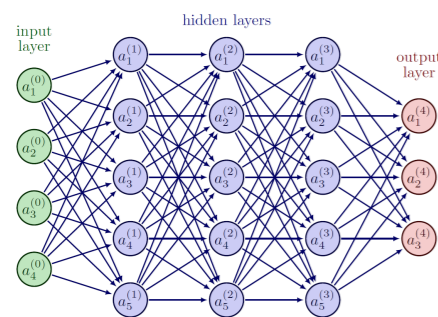
Strategy:

- Replace the part most affected by uncertainty by neural networks
- General formulation applying specific constrains
- Example of application to a mass balance model: the ALBA model

Application:

- Pre-training neural network: determining a first set of parameters → **static approach**
- Training techniques based on back propagation: closing the gap between model and real data → **dynamic approach**

$$\dot{\xi} = K \cdot \rho(\xi, T, \theta, \hat{H}^+) + \Delta(\xi, \xi_{in}, T, \hat{H}^+)$$

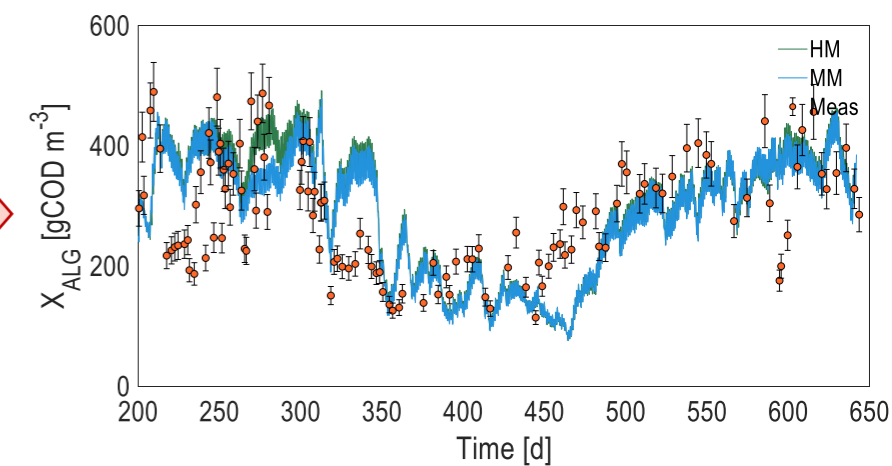


Mass conservation

$$\forall \eta \in \{C, N, P, O, H\} \exists \lambda_\eta > 0 \in Ker(K^T) \mid \lambda_\eta^T K = 0$$

$$\Psi = \lambda_\eta^T \xi \rightarrow \text{mass of the total element } \eta \text{ in the system}$$

$$\dot{\Psi} = \lambda_\eta^T K \rho(\xi, T, \theta, \hat{H}^+) + \lambda_\eta^T \Delta(\xi, \xi_{in}, T, \hat{H}^+)$$



1ST PHASE: CONSTRAINED STATE BOUNDARY

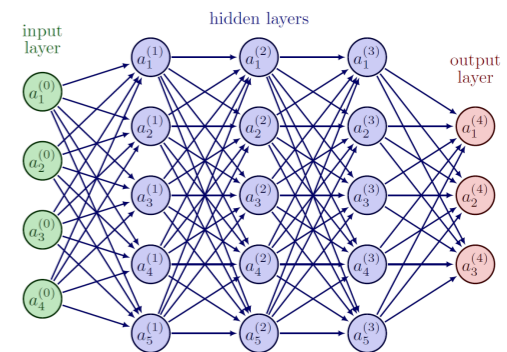
First level of hybridization

$$\frac{d\xi}{dt} = Kr(\xi, u) + D(\xi_{in} - \xi) - Q(\xi, u)$$

Which structure for the kinetics would guaranty the trajectory to respect

- physical positivity of the concentrations
- causality (i.e. no substrate: no reaction)

$$r_i(\xi, u) = C(\xi) \omega(\xi, u)$$



Unknown part given by the NN

$$\omega_i(\xi, u) = \sigma \left(\sum_{i=1}^n w_{1,i} a_i^{(L)} + b_1^{(0)} \right)$$

Constrain function (containing) $\prod_k \xi_k$

Such that: $\xi_i = 0 \Rightarrow \dot{\xi}_i \geq 0$



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2ND PHASE: KINETIC IDENTIFICATION

Second level of hybridization

Computing the target functions from the trajectories of the mechanistic model:

$$\omega_i^{MM}(\xi^{MM}, u) = \frac{\rho_i^{MM}}{C_i(\xi^{MM})}$$

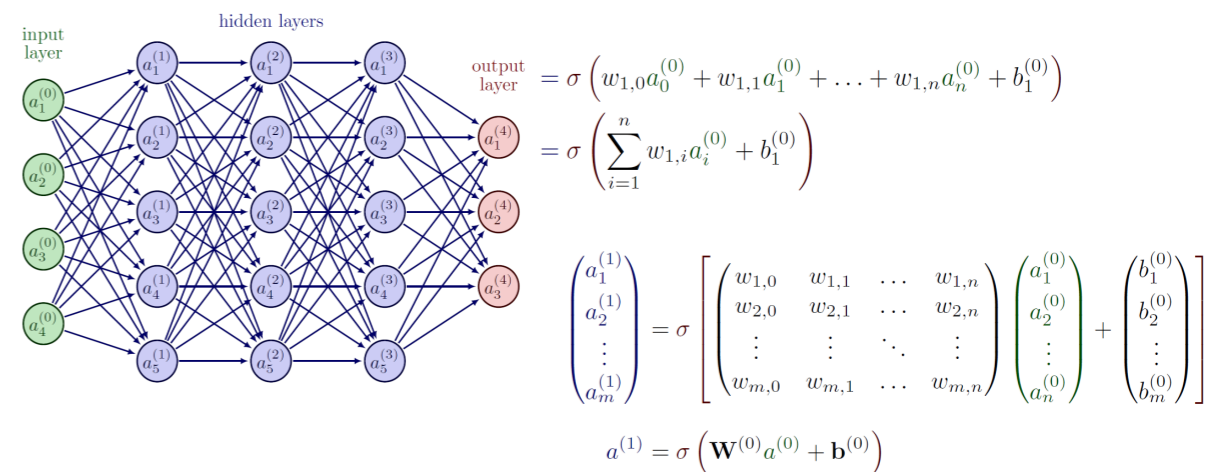
Generated by the mechanistic model

Chosen constrain function

Static problem: Loss function (Ω : parameters of the Neural Network)

$$\mathcal{L}_i(\Omega) = \sum_j \left(\omega_i^{NN}(\Omega, \xi^{MM}(t_j), u) - \omega_i^{MM}(\xi^{MM}(t_j), u) \right)^2$$

$$\sigma \left(\sum_{i=1}^n w_{L+1,i} a_i^{(L+1)} + b_1^{(L+1)} \right)$$

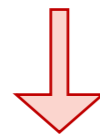


2ND PHASE: KINETIC IDENTIFICATION

Application to the ALBA model

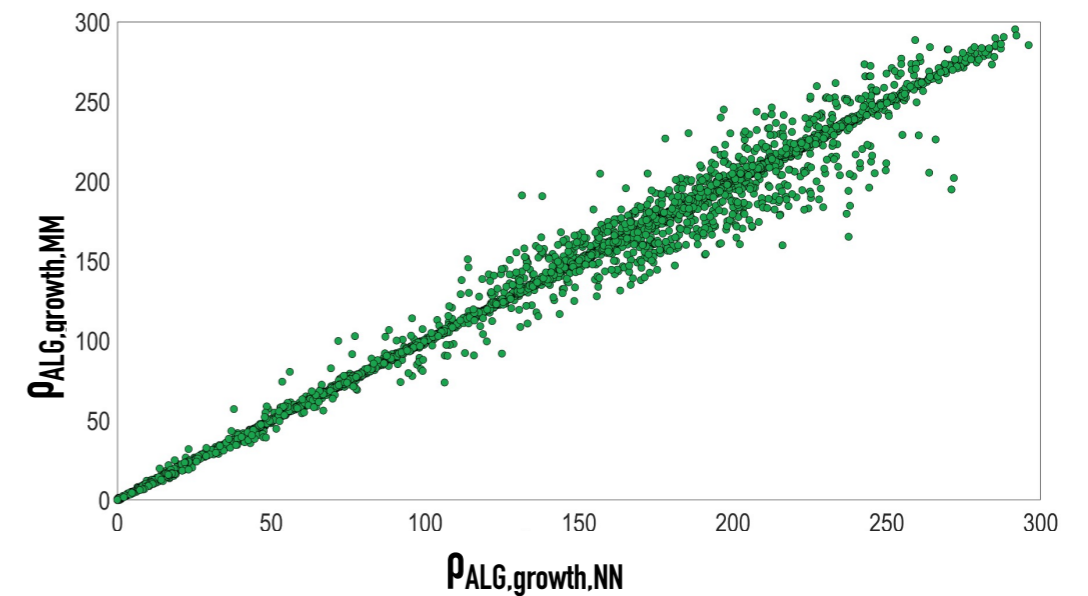
Identifying a neural network structure for every biological kinetic

Hidden layers structure	Parameters (weights for one kinetic)	Parameters (weights for all the kinetic)	Input	Target
7-7-7	252	4788	21	$\rho_{i,MM}$



Hidden layers structure	Mean error (10k iteration)	Performance test
5-3-2	0.0115	3.5e-04
7-7-7	0.0029	3.5e-04
7	0.0272	4.5e-04

Learning of function $\omega_1(\xi, u)$



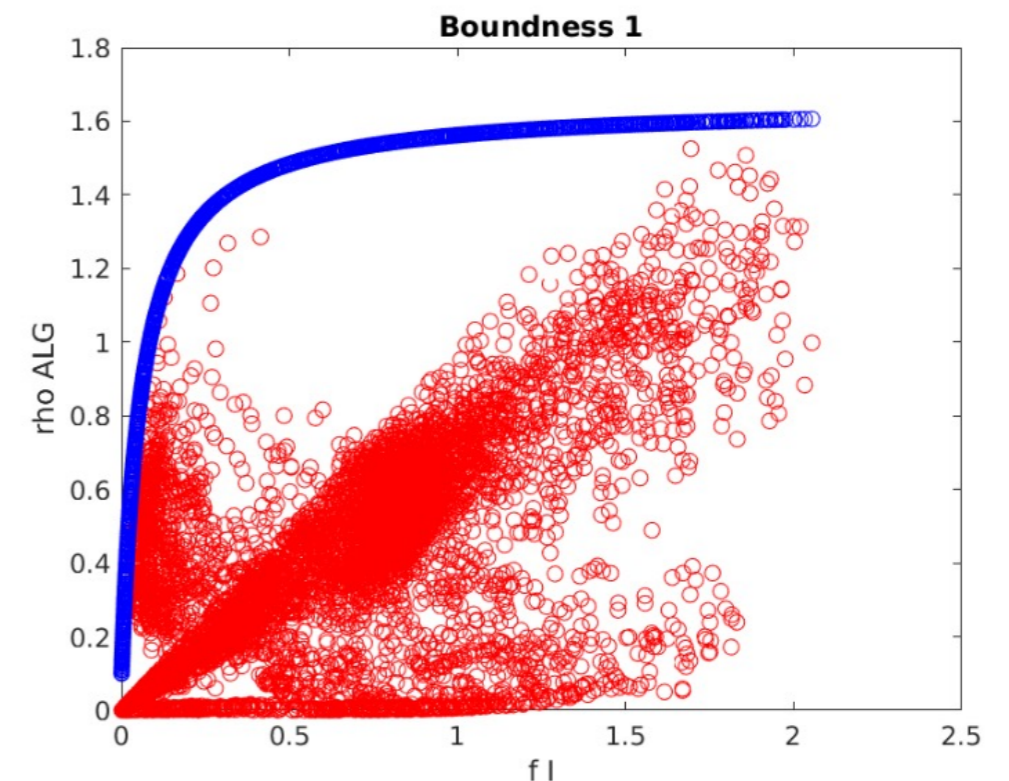
- Training the neural network based on the simulated mechanistic kinetics
- Advantage: with the model we can generate a wide range of conditions and points!

3RD PHASE : KINETIC BOUNDARIES

Creation of functions to bound the bio-kinetic rates (derived from the MM simulation):

- Non negative bio-kinetic reats (min boundary)
- Not too high values → not realistic (max boundary)
- Can also be derived by expert knowledge on the kinetics

$$\rho_i^{NN}(\Omega, \xi, u) \leq \mathcal{P}_i(\xi, u)$$



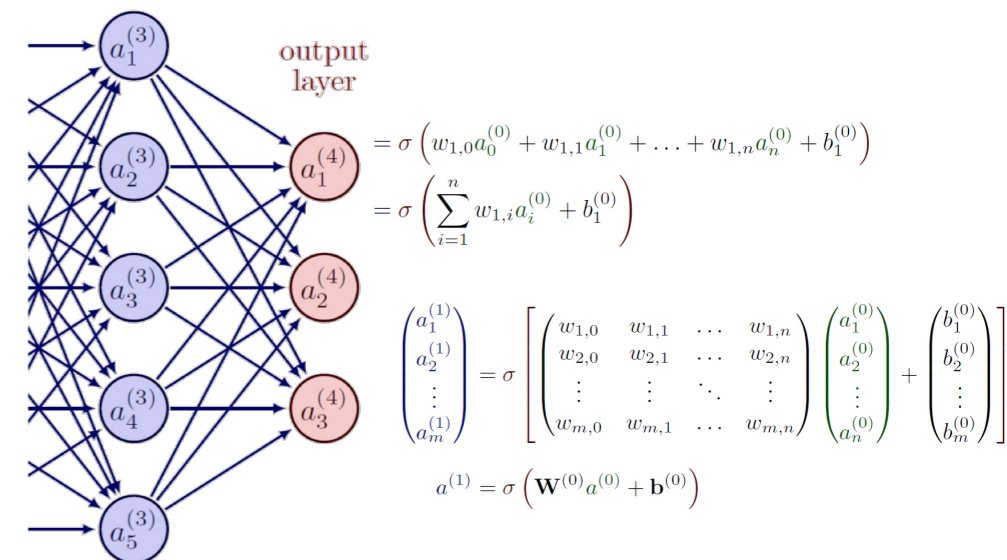
Saturation of the NN prediction: guarantees the predicted kinetics do not become weird far from the training data set.

4TH PHASE : FINE TUNING

Fine tuning of a subset of the NN parameters with the experimental data using dynamic backpropagation

Loss function ($\tilde{\Omega}$: subset of the parameters Ω from the Neural Network):

$$\tilde{\mathcal{L}}(\tilde{\Omega}) = \sum_{i,j} \left(\xi_i^{NN}(t_j, \tilde{\Omega}) - \xi_i^{Meas}(t_j) \right)^2$$



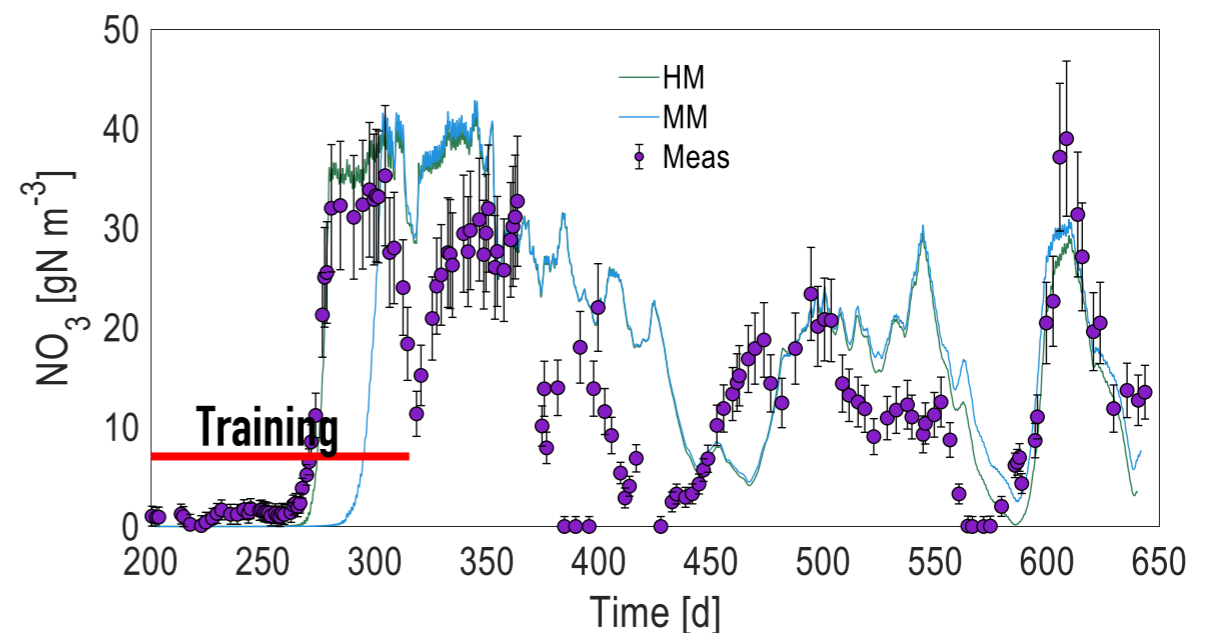
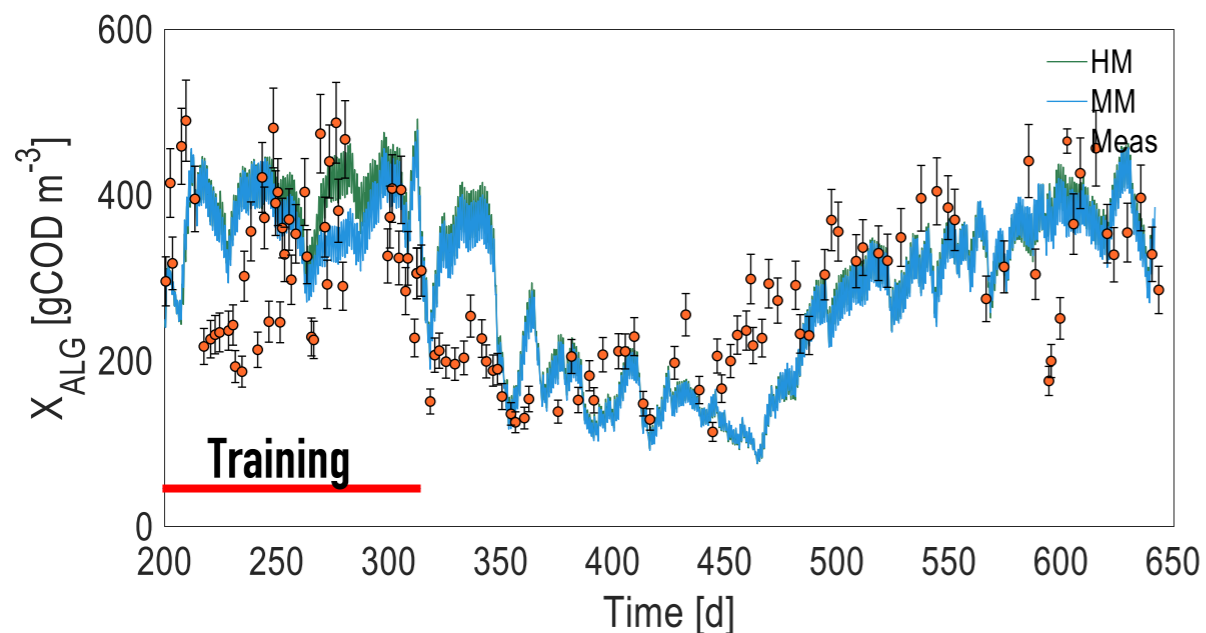
The gradient $\vec{\text{grad}}(\Omega) = \frac{\partial \mathcal{L}}{\partial \Omega}$ is computed with a backpropagation approach, based on an estimate of the sensitivity function $\sigma_{\Omega} = \frac{\partial \xi}{\partial \Omega}$

The algorithm starts from the parameter Ω t estimated in phase 2.

4TH PHASE : FINE TUNING

Application to the ALBA model

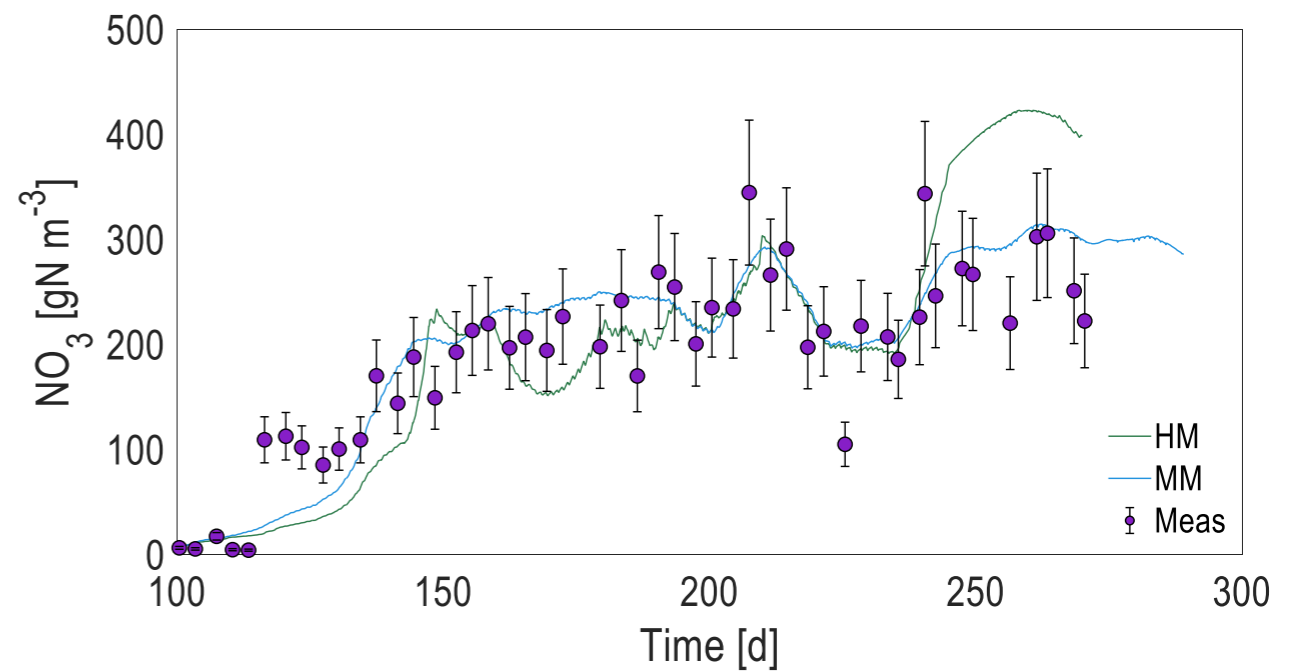
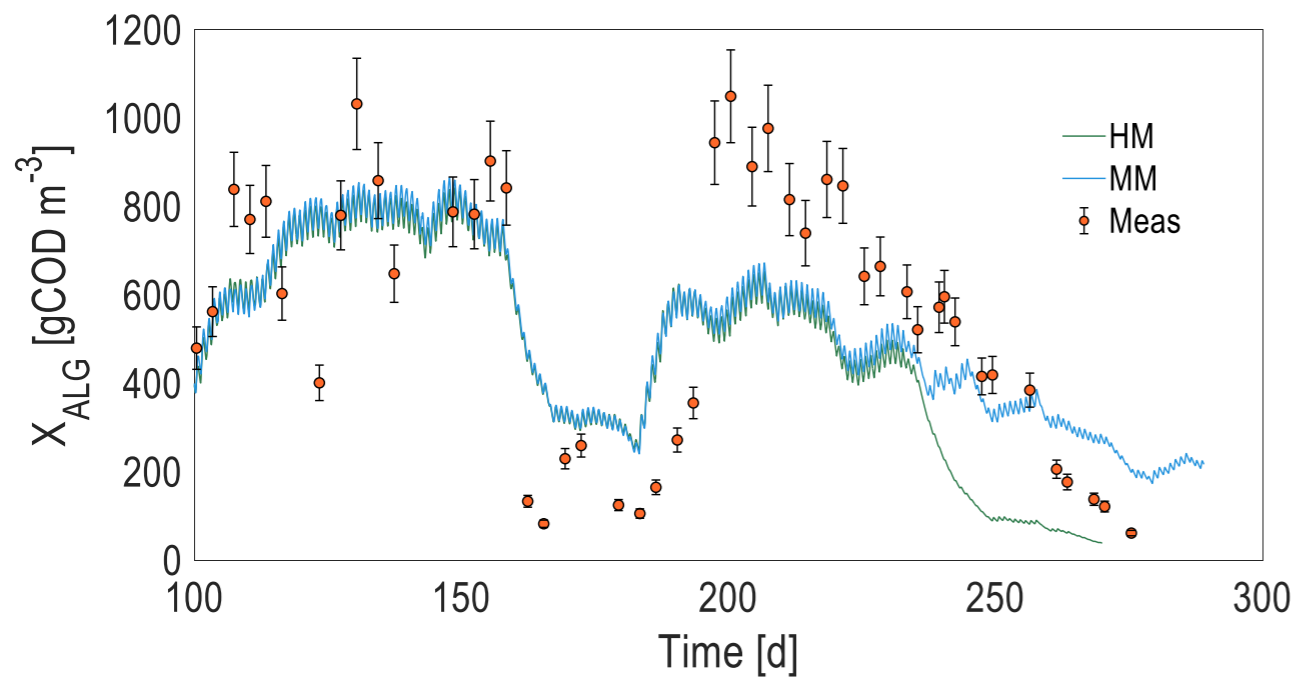
Fine tuning using on-line O_2 and measurements of algal biomass and inorganic nitrogen



Fit improvement in the training period

5TH PHASE: VALIDATION AND TEST

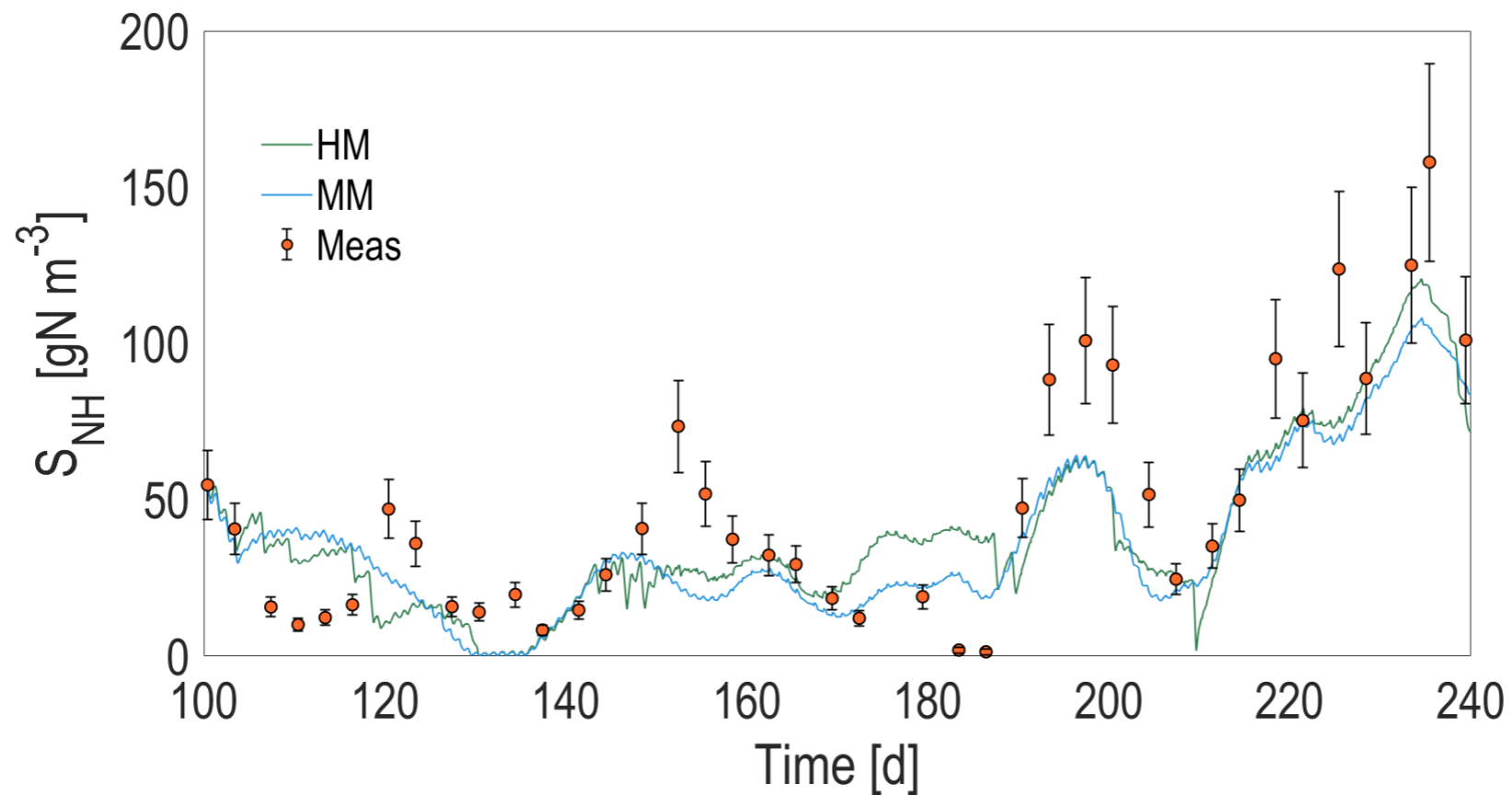
Application to the ALBA model for predicting another case (Milan)



Test phase: different dataset not used for the training

5TH PHASE: VALIDATION AND TEST

Application to the ALBA model for predicting another case (Milan)



NH_4^+ is very challenging to predict

Test phase: different dataset not used for the training

- Understanding the rules driving response to temperature in phytoplankton (O. Bernard)
- Neural ODE for representing phytoplankton growth driven by light (I. Fierro)
- Towards hybrid modelling of artificial microbial ecosystems (F. Casagli)
- **Spatio-temporal high-resolution models of particulate organic matter abundance in the ocean (R. Ranini)**

Effect of temperature and light on phytoplankton growth

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Olivier BERNARD, ...AGLI, Romain RANINI, Ignacio FIERRO, Jineth ARANGO, Kilian BURGI, David JEISON, Antoine SCIANDRA, Lionel GUIDI



Inria



Green Owl

OPTIMISATION OF WATER LIVING MICROORGANISMS FOR
GENERATING
RENEWABLE RESOURCES

Olivier BERNARD

